Comparison of different impulse response measurement techniques

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Abstract

The impulse response of an acoustical space or transducer is one of their most important characterization. In order to perform the measurement of their impulse responses, four of the most suited methods are compared: MLS (Maximum Length Sequence), IRS (Inverse Repeated Sequence), Time-Stretched Pulses and SineSweep. These different methods have already been described in the literature. Nevertheless, the choice of one of these methods depending on the measurement conditions is critical. Therefore, an extensive comparison has been realized. This comparison has been done through the implementation and realization of a complete, fast, reliable and cheap measurement system. Finally, a conclusion for the use of each method according to the principal measurement conditions is presented. It is shown that in the presence of non white noise, the MLS and IRS techniques seem to be more accurate. On the contrary, in quiet environments the Logarithmic SineSweep method seems to be the most appropriate.

1 Introduction

Under the assumption of source and receiver immobility, the acoustical space in which they are placed can be considered as a Linear and Time Invariant system characterized by an impulse response $h(t)$. In room acoustics, the accurate measurement of the impulse response is very important, since many acoustical parameters can be derived from it. Moreover, in nowadays audio applications (i.e. virtual reality, auralization, spatialization of sounds), the importance of measuring binaural room impulse responses with a very high signal-to-noise ratio becomes more and more evident. Once the impulse response has been measured precisely, it can be integrated in a complete auralization process ([1], [2]). In order to achieve the best quality for this auralization process, the measured impulse response must reach a very good signal-to-noise ratio (more than 80 dB if possible).

A common method for measuring the impulse response of such an acoustical system is to apply a known input signal and to measure the system’s output. The choice concerning the excitation signal and the deconvolution technique enabling the obtention of the impulse response from the measured output is of essential importance:

- The emitted signal must be perfectly reproducible.

- The excitation signal and the deconvolution technique have to maximize the signal-to-noise ratio of the deconvolved impulse response.

- The excitation signal and the deconvolution technique must enable the elimination of non linear artifacts in the deconvolved impulse response.

In general, the signal-to-noise ratio is improved by taking multiple averages of the measured output signal before the impulse response deconvolution process is started.

The most commonly used excitation signals are deterministic, wide-band signals known as:

- MLS (Maximum Length Sequence) and IRS (Inverse Repeated Sequence) which use pseudo-random white noise.

- Time-Stretched Pulses and SineSweep which use time varying frequency signals.
2 Brief description of the four measurement techniques

The acoustical impulse response measurements using the MLS technique were first proposed by Schroeder in 1979 ([3]) and have been used for more than twenty years. Many papers discussed its theoretical and practical advantages and inconveniences ([4], [5], [6], [7], [8], [9], [10], [11], [12], [13], [14], [15]). Shortly after the paper of Schroeder, the IRS technique was proposed as an alternative allowing a theoretical reduction of the distortion artifacts introduced by the MLS technique ([4], [16], [17]).

Two years after the proposition of Schroeder, Aoshima introduced a new idea for the measurements of impulse responses which led to the time-stretched pulses technique ([18]). His idea was then pushed further in the paper of Suzuki et al. ([19]) proposing what they called an “Optimum computer-generated pulse signal”.

Recently, Farina introduced the logarithmic SineSweep technique ([20], [21]) intended to overcome most of the limitations encountered in the other techniques. The idea of using a sweep in order to deconvolve the impulse response is not new ([22]) but the deconvolution method used is different in the paper of Farina.

These techniques have already been described and discussed in many papers. However, it is intended here to focus on some important properties which are necessary to understand the comparison of the different methods.

2.1 MLS Technique

The MLS technique is based upon the excitation of the acoustical space by a periodic pseudo-random signal having almost the same stochastic properties as a pure white noise. The number of samples of one period of an order MLS signal is: \( L = 2^m - 1 \).

More theoretical considerations about the MLS sequences can be found in: [7], [10], [12], [13], [23] and in the excellent book on the shift-register theory [24].

With the MLS technique, the impulse response is obtained by circular cross-correlation (as shown in [25]) between the measured output and the determined input (MLS sequence). Because of the use of circular operations to deconvolve the impulse response, the MLS technique delivers the periodic impulse response \( h'[n] \) which is related to the linear impulse response by the following equation:

\[
    h'[n] = \sum_{l=-\infty}^{+\infty} h[n + lL]
\]

Equation (1) reflects the well known problem of the MLS technique: the time-aliasing error. This error is significant if the length \( L \) of one period is shorter than the length of the impulse response to be measured. Therefore, the order \( m \) of the MLS sequence must be high enough in order to overcome the time-aliasing error. Our measurement system allows generation of MLS sequences up to order 19 (which corresponds to a period of 12 seconds if the sampling frequency is 44.1 kHz).

2.1.1 MLS Immunity to signals not correlated with the excitation signal

Each MLS sequence is characterized by a phase spectrum which is strongly erratic, with a uniform density of probability in the \([-\pi, +\pi]\) interval as can be seen in figure 1.

According to this property, the MLS technique is able to randomize the phase spectrum of any component of the output signal which is not correlated with the MLS input sequence ([5], [9]). As a consequence, any disturbing signal (i.e. white or impulsive noise) will actually be phase randomized, and this will lead to a uniform repartition of the disturbing effects along the deconvolved impulse response (see figures 2 and 3) instead of localized noise contributions along the time axis. A post-averaging method can then be used in order to reduce this uniformly distributed noise appearing in the deconvolved impulse response.

2.1.2 Inconveniences of the MLS technique

The major problem of the MLS method resides in the appearance of distortion artifacts known as “distortion peaks” ([6]). These artifacts are more or less uniformly distributed along the deconvolved impulse response. The origin of the distortion peaks lies in the non linearities inherent to the measurement system and especially to the loudspeaker.

These distortion artifacts introduce characteristic crackling noise when the measured impulse response is convolved with some anechoic signal in order to realize the auralization process. These distortion peaks can be attenuated by:

- The use of dedicated measurement methods (such as the Inverse Repeated Sequence technique ([4], [16])).
- The optimization of some measurement parameters. For example, the amplitude of the excitation signal is, in practice, a compromise between increasing distortions at high levels and decreasing the signal-to-noise ratio at low levels. This optimization is very time consuming because of the practical difficulty to find the optimal amplification level. Moreover, this compromise level must be carefully chosen for each new measurement situation.
Figure 5 illustrates the quality of the results that can be obtained when particular care is taken for the optimization of the parameters (mainly the output level) conditioning the MLS (or IRS) input signal. It can be seen that the distortion peaks are significantly reduced but not completely removed.

2.2 IRS technique

Each IRS sequence with a 2L samples period \((x[n])\) is defined from the corresponding MLS sequence of period \(L\) \((mls[n])\) by the following relation:

\[
x[n] = \begin{cases} 
    mls[n], & \text{if } n \text{ is even, } 0 \leq n < 2L \\
    -mls[n], & \text{if } n \text{ is odd, } 0 < n < 2L 
\end{cases}
\]  

(2)

The deconvolution process is exactly the same as for the MLS technique (circular correlation).

Figure 4 shows the attenuation of the distortion peaks when the IRS method is used. These impulse responses have been obtained by performing the measurements in an anechoic room leaving all measurement parameters unchanged from one measure to the other.

2.3 Time-Stretched Pulses technique

This method is based on a time expansion and compression technique of an impulsive signal ([18]). The aim of using an expansion process for the excitation signal is to increase the amount of sound power emitted for a fixed magnitude of this signal and therefore to increase the signal-to-noise ratio without increasing the nonlinearities introduced by the measurement system. Once the response to this “stretched” signal has been measured, a compression filter is used in order to compensate for the induced stretching effects and to obtain the deconvolved impulse response.

Figure 6 shows the impulse response obtained with this technique. The magnitude scale has been enlarged to clearly illustrate the absence of distortion peaks. However, this does not mean that distortion artifacts are completely removed. They still appear in the impulse response (as a residue of the deconvolution filter) as can be seen on figure 7.

2.4 Logarithmic SineSweep technique

The MLS, IRS and Time-Stretched Pulses methods rely on the assumption of LTI (Linear, Time-Invariant) Systems and cause distortion artifacts to appear in the deconvolved impulse response when this condition is not fulfilled.

The SineSweep technique developed by Farina ([21]) overcomes such limitations. It is based on the following idea: by using an exponential time-growing frequency sweep, it is possible to simultaneously deconvolve the linear impulse response of the system and to selectively separate each impulse response corresponding to the harmonic distortion orders considered. The harmonic distortions appear prior to the linear impulse response. Therefore, the linear impulse response measured is assured exempt from any non linearity and, at the same time, the measurement of the harmonic distortion at various orders can be performed.

Figure 8 illustrates the black box modelization of the measurement process common to all four techniques discussed in this paper. In this modelization it is assumed that the measurement system is intrinsically not linear but, on the other hand, perfect linearity is considered regarding the acoustical space from which the impulse response is to be derived.

As pointed out by Farina ([21]), the signal emitted by the loudspeaker is composed of harmonic distortions (considered here without memory) and may be thus represented by the following equation (see figure 8):

\[
w(t) = x(t) \otimes k_1(t) + x^2(t) \otimes k_2(t) + x^3(t) \otimes k_3(t) + \ldots + x^N(t) \otimes k_N(t)
\]  

(3)

where \(k_i(t)\) represents the \(i^{th}\) component of the Volterra Kernel ([21]) which takes into account the nonlinearities of the measurement system.

In practice, it is relatively difficult to separate the linear part (reverberation part in the impulse response) from the non linear part (distortions). In the following, we will consider the response of the global system (the output signal from the system represented in figure 8) as being composed of an additive gaussian white noise \((n(t))\) and a set of impulse responses \((h_i(t))\), each of them being convolved by a different power of the input signal.

\[
g(t) = n(t) + x(t) \otimes h_1(t) + x^2(t) \otimes h_2(t) + x^3(t) \otimes h_3(t) + \ldots + x^N(t) \otimes h_N(t)
\]  

(4)

where \(h_i(t) = k_i(t) \otimes h(t)\).

Equation (4) underlines the existence of the non linearities at the system’s output.

In the case of the logarithmic SineSweep technique, the excitation signal is generated on the basis of the following equation (see [21] for more theoretical informations):
\[ x(t) = \sin \left[ \frac{T \omega_1}{\ln(\omega_2/\omega_1)} \left( e^{\frac{1}{\ln(\omega_2/\omega_1)}} - 1 \right) \right] \] (5)

where \( \omega_1 \) is the initial radian frequency and \( \omega_2 \) is the final radian frequency of the sweep of duration \( T \).

Figure 9 shows the time and spectral representations of a logarithmic sweep with initial and final frequency at 10 Hz and 1000 Hz respectively.

The impulse response deconvolution process is realized by linear convolution of the measured output with the analytical inverse filter preprocessed from the excitation signal. Using linear convolution allows time-aliasing problems to be avoided. In fact, even if the time analysis window has the same length as the emitted SineSweep signal (and is shorter than the impulse response to be measured), the tail of the system response may be lost, but this will not introduce time aliasing. This is a first advantage upon MLS and IRS methods.

In practice, a silence of sufficient duration is added at the end of the SineSweep signal in order to recover the tail of the impulse response.

The deconvolution of the impulse response requires the creation of an inverse filter \( f(t) \) able to "transform" the initial Sweep into a delayed Dirac’s delta function:

\[ x(t) \otimes f(t) = \delta(t - K) \] (6)

The deconvolution of the impulse response is then realized by linearly convolving the output of the measured system \( y(t) \) with this inverse filter \( f(t) \):

\[ h(t) = y(t) \otimes f(t) \] (7)

The Inverse Filter \( f(t) \) is generated in the following manner:

1. The Logarithmic Sweep (which is a causal and stable signal) is temporally reversed and then delayed in order to obtain a causal signal (the reversed signal is pulled back in the positive region of the time axis). This time reversal causes a sign inversion in the phase spectrum. As such, the convolution of this reversed version of the excitation signal with the initial SineSweep will lead to a signal characterized by a perfectly linear phase (corresponding to a pure delay) but will introduce a squaring of the magnitude spectrum.

2. The magnitude spectrum of the resulting signal is then divided by the square of the magnitude spectrum of the initial SineSweep signal.

The time and spectral representations of the Inverse Filter corresponding to the SineSweep (fig. 9) is given in figure 10.

In order to minimize the influence of the transients introduced by the measurement system and appearing at the beginning and the end of the emission of the excitation signal, the ends of the SineSweep signal are exponentially attenuated (exponential growth at the beginning and exponential decrease at the end).

In order to perform acoustical measurements on all the audible range, the excitation signal must extend from 20 Hz to 20000 Hz. As the transients have to be included out of this range, the choice of \( f_1 = 10 \) Hz (initial sweep frequency) and \( f_2 = 22000 \) Hz (final sweep frequency) is realized.

In practice, the SineSweep deconvolution leads to the apparition of a sequence of impulse responses clearly separated along the time axis (fig. 11). It is shown in figure 11 that the different harmonic distortion orders appear separately before the “linear impulse response” in increasing orders, from right to left.

3 Implementation and experimental setup

3.1 Measurement system

A complete measurement system has been designed and realized to enable fast, reliable and simple comparisons between the different methods.

Of course several dedicated measurement systems already exist, but these are generally expensive, immutable (because of the hardware implementation of the algorithms) and bulky. Therefore, a graphical, highly configurable, portable program written under MATLAB 5.3 has been developed for the automatic acquisition of the impulse response with common elements such as a microphone, a loudspeaker and a computer. This has led to the obtention of a global, cheap and adaptable measurement system (see figure 12) allowing fast and accurate measurement of the impulse response.

The MATLAB program controls the generation of the different excitation signals, their emission through the loudspeaker connected via the power amplifier to the full-duplex soundcard, and the simultaneous recording of the signal at the microphone. The deconvolution technique is then automatically performed. The time required for one measurement is very short: only a few seconds are necessary to obtain the impulse response of an acoustical space.
3.2 Room impulse response acquisition

In order to accurately measure room impulse responses, the measurement system characteristics must be taken into consideration.

The calibration of the whole measurement chain requires an inverse filtering correction which, in this case, is realized by the application of the “Time Reversal Mirror Filter” technique ([26]). This last technique generates a pre-equalized excitation signal in three steps:

1. Acquisition of the measurement system impulse response in an anechoic room (for example by using one of the technique described earlier).

2. Time reversal of the system impulse response after appropriate truncation and addition of a time delay in order to obtain a causal result\(^1\). This “reversed” impulse response is linearly convolved with the excitation signal (MLS, sweep, ...) that has to be pre-equalized.

3. Division of the spectrum magnitude of the signal obtained in step 2 by the square of the measurement system magnitude response (Fast Fourier Transform of the impulse response obtained in step 1).

The results of the pre-equalization technique are presented in figure 13. It can be seen that the phase spectrum is perfectly linear and the amplitude spectrum is almost constant (the residual oscillations around the mean value do not exceed ±0.4 dB) in the range between 40 Hz and 18 kHz.

4 Comparison of the four methods

The comparison of the four impulse response measurement methods has been first realized in the anechoic room in order to insure individual control of the set of parameters conditioning the measurement. The characteristic parameters of each method have been chosen in order to allow an objective comparison: for example, the duration of the excitation signals and the number of averages used have been maintained constant during all measurements.

The program written under MATLAB allows the following parameters to be modified:

Parameters common to all methods:

- sampling frequency
- number of averages (i.e. number of times the emitted signal will be send to the loudspeaker)
- Recording mode: mono or stereo (for example for Head Related Impulse Responses measurements)

Parameters specific to each method:

**MLS**

Order of the MLS sequence (Maximum order = 19; number of samples contained in one period of an \(m\) order MLS sequence=\(2^m - 1\))

**IRS**

Order of the IRS sequence (Maximum order = 19; number of samples contained in one period of an \(m\) order IRS sequence=\(2 \ast (2^m - 1)\))

**Time-Stretched Pulses**

- Total duration of the pulse
- Stretching percentage (indication of the ratio between the amount of time during which the pulse has a non negligible amplitude and the total duration of the pulse)

**SineSweep**

- initial frequency
- final frequency
- sweep duration
- duration of the silences inserted after each sweep

Figure 14 illustrates the disposition of the transducers in the anechoic room in order to compare the different measurement techniques.

\(^1\)The aim of this step is to inverse the phase polarity of the signal.
4.1 Optimal parameters

Figure 15 gives a general survey of the impulse responses measured with the four methods presented above when the measurement parameters (i.e. amplification sound level) have been optimized individually for each measurement technique. The magnitude scale has been enlarged in order to focus on the residual noise present.

The reverberation time and the ambient noise level in the anechoic chamber being very low, the choice of a MLS sequence of order 16 seemed to be a reasonable compromise between measurement time and good signal-to-noise ratio. The durations of the excitation signals used in the other measurement methods have then been adjusted according to the duration of the MLS excitation signal (i.e. 1.5 seconds for a sampling frequency of 44100 Hz).

Thus, in order to obtain comparable measurements, the following parameters were used:

- sampling frequency : 44100 Hz
- MLS and IRS sequence orders : 16 (corresponding to signals of 1.5 and 3 seconds respectively, according to the chosen sampling frequency)
- output amplification level : optimized in accordance with the method used by trial-error adjustment of the amplifier knob (the different levels used are listed in table 1)
- Time-Stretched Pulses duration : 1.5 seconds
- Time-Stretched Pulses stretch percentage : 80 %
- Initial and final SineSweep frequencies : $f_1 = 10$ Hz and $f_2 = 22000$ Hz
- SineSweep duration : 1.5 seconds
- No averaging
- Noise level in the anechoic room when the computer is present : 30 dB

When the measurement parameters are optimized, the differences between the MLS and IRS methods tend to vanish (see figures 15 (a) and 15 (b)). Furthermore, the use of a relatively low output level and the timbre (a white noise is less disturbing than a sweep) of these methods is an advantage if the measurements are to be made in occupied rooms. The advantage of the IRS technique may still be considered : for example, on the extreme right of the figure 15 (b) the peak existing in figure 15 (a) has disappeared.

The disappearance of the distortion peaks when the Time-Stretched Pulses method is used is clearly shown on figure 15 (c).

Finally, the perfect separation of the harmonic distortions from the linear impulse response when the SineSweep method is used is evident on figure 15 (d).

The advantage of this last method lies in the fact that the obtention of optimal results does not necessitate a tedious optimization process of the measurement parameters since the limitation about the output amplification level in order to avoid significant distortions does not exist anymore (the non superposition of the tail of the impulse response corresponding to the second order distortion with the linear impulse response is the only precaution that has to be taken by choosing a sufficient duration of the SineSweep signal ([21])).

On figure 15 the time axes have not the same origin in order to focus on details particular to each method.

4.2 Signal-to-noise ratio

In order to perform an objective comparison of the impulse response qualities, the optimal signal-to-noise ratios achievable for each technique have been compared. In the following, the signal-to-noise ratio definition used is the ratio expressed in dB between the average power of the signal recorded by the microphone and the average power of the noise and distortions present in the tail of the deconvolved (linear) impulse response. Obviously, we might expect a better signal-to-noise ratio for the sinewave method since there are no distortions artifacts present in the tail of the deconvolved (linear) impulse response. This affirmation is confirmed by the results presented in table 2.

<table>
<thead>
<tr>
<th>Method</th>
<th>Optimal Sound Level</th>
</tr>
</thead>
<tbody>
<tr>
<td>MLS</td>
<td>75.5 dB</td>
</tr>
<tr>
<td>IRS</td>
<td>75.5 dB</td>
</tr>
<tr>
<td>Time-Stretched Pulses</td>
<td>83.9 dB</td>
</tr>
<tr>
<td>SineSweep</td>
<td>92.5 dB</td>
</tr>
</tbody>
</table>

Table 1: Optimal values of the sound levels at the position of the microphone for each measurement method.
Table 2: Optimal signal-to-noise ratios for each method.

<table>
<thead>
<tr>
<th>Method</th>
<th>Optimal Signal-to-Noise Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>MLS</td>
<td>60.5 dB</td>
</tr>
<tr>
<td>IRS</td>
<td>63.2 dB</td>
</tr>
<tr>
<td>Time-Stretched Pulses</td>
<td>77.0 dB</td>
</tr>
<tr>
<td>SineSweep</td>
<td>80.1 dB</td>
</tr>
</tbody>
</table>

Table 2 shows the optimal signal-to-noise ratios (i.e., the signal-to-noise ratios obtained when the measurement parameters have been optimized) for each of the four methods presented above.

Bleakley and Scaife ([11]) have showed that the signal-to-noise ratio for the MLS sequence increases by 3dB when the period length of the MLS sequence is doubled. It is thus logical to obtain a 3 dB gain for the IRS technique in comparison to the MLS since the length of an IRS sequence is twice the length of the corresponding (same order) MLS sequence.

The noticeable gain of 14 dB of the Time-Stretched Pulses method on the IRS method can be explained by the use of an optimal output sound level far above the one used in the MLS or IRS cases, as well as by the disappearance of the spurious distortion peaks.

Finally, the excellent signal-to-noise ratio (80 dB) obtained with the SineSweep technique is due to the total rejection of the non linear distortion artifacts prior to the linear impulse response. The output signal level is not limited anymore by the need to reduce the non linear influence since all non linear distortions are measured separately. This leads to the best optimal signal-to-noise ratio (20 dB better than for the MLS method).

4.3 Impulsive noise Immunity

Figure 16 shows the impulse responses obtained when measurements are performed in an environment where impulsive noise is simultaneously present. The IRS method gives results approximately identical to those of the MLS technique and thus its corresponding impulse response is not shown here. As previously announced, only the pseudo-random noise techniques (MLS and IRS) possess the ability of randomizing the phase of any component in the recorded signal that is not correlated to the input signal emitted in the acoustical space. Thus, any additional noise (white or even impulsive) will be uniformly distributed along the deconvolved impulse response. Therefore, additive impulsive noise (appearing as additive white noise in the deconvolved impulse response) is subject to posterior attenuation by averaging techniques.

On the contrary, the presence of impulsive noise when the Time-Stretched Pulse or SineSweep techniques are used, heavily compromises the impulse response deconvolution process through the presence of excitation signal residues in the deconvolved impulse response. These residues being strongly correlated with the excitation signal will not be properly eliminated if posterior average techniques are used.

As a first conclusion, we may say that in a (non random) noisy environment, the MLS (IRS) method is subject to give better results than the other two.

4.4 Impulse response measurements in classical rooms

The properties described above were mostly illustrated by measurements performed in anechoic rooms. In this section we will show the results given when the measurements are performed in more classical rooms such as auditoria or lecture rooms.

As can be seen on figure 18, most of the properties that have been illustrated in the case of anechoic measurements are still visible. We can particularly focus on the separation of the different harmonic distortions from the linear impulse response in the case of the SineSweep technique. In this case, the impact of reverberation on each impulse response can be clearly seen and illustrates the need for non superposition of the second order distortion with the linear impulse response by using a sufficiently long SineSweep.

5 Conclusions

A complete, cheap and parametrizable measurement system has been realized in order to compare different impulse response measurement methods. This system is based on a computer program written under MATLAB 5.3 allowing an automatic and easy measurement to be realized. On the basis of this measurement system, a comparison of four different methods has been done.

The comparison of the four methods leads us to the following conclusions:

1. The MLS (IRS) method seems the most interesting method when the measurements have to be performed in an occupied room or in exterior due to its strong immunity to all kinds of noise (white, impulsive or others), its weak optimal output sound level and its timbre (white noise is more supportable and easily
masked out than sweep signals). However, its major drawback lies in the tedious calibration that has to be carried out to obtain optimal results and in the appearance of spurious peaks ("distortion peaks") due to the inherent non-linearities of the measurement system.

2. The Time-Stretched Pulses method avoids the appearance of the distortion peaks. However, the remaining non-linear artifacts can possibly be superimposed with the deconvolved "linear" impulse response. The presence of a residue of the excitation signal in the deconvolved impulse response is a result of such superposition problem. This residue can be almost completely eliminated if a precise calibration of the measurement parameters (mainly the output level) is realized. However, its timbre and the high value of the optimal output signal level needed to mask out the ambient noise makes it unusable in occupied rooms.

3. The perfect and complete rejection of the harmonic distortions prior to the "linear" impulse response, their individual measurement and the excellent signal-to-noise ratio of the SineSweep method make it the best impulse response measurement technique in an unoccupied and quiet room. Moreover, unlike the preceding methods, it does not necessitate a tedious calibration in order to obtain very good results (no compromise between the signal-to-noise ratio and the superposition of non-linear artifacts in the room impulse response). However, as for the Time-Stretched Pulses method, the SineSweep technique is not recommended for measurements in occupied rooms.

References

Figure 1: Magnitude and Phase Spectra of an MLS sequence. The phase spectrum has been enlarged in order to clearly show its uniform random distribution.


Figure 2: (a) Impulse response of a classroom obtained with a single MLS sequence of order 18 when a white noise generator is simultaneously present. The Noise Level measured at the position of the microphone is 60 dB. (b) Zoom on the end of the impulse response.

Figure 3: (a) Impulse response obtained with a single MLS sequence of order 16 in an anechoic room when Impulsive Noise is simultaneously present. (b) Zoom on the magnitude scale.

Figure 4: Zoom on the impulse responses obtained via MLS and IRS methods. (a) MLS method. (b) IRS method.
Figure 5: Zoom on the impulse response obtained when optimization of the measurement parameters (i.e. output sound level) of the MLS technique is realized.

Figure 6: Zoom on the impulse response of a classroom obtained when a time-stretched pulse of about 6 seconds is used.

Figure 7: Zoom on the impulse response obtained in an anechoic room when a time-stretched pulse of about 1 second is used. In this case a bad quality loudspeaker has been used in order to emphasize the non linearity of the measurement system.
Input Signal $x(t)$  
\[ \text{Non Linear System} \quad K[x(t)] \]  
\[ \text{Distorted Signal} \quad w(t) \]  
\[ \text{Linear System} \quad w(t) \otimes h(t) \]  
\[ \text{Output Signal} \quad y(t) \]  
\[ \text{Noise} \quad n(t) \]

Figure 8: Modelization of the global system including the loudspeaker (considered as a non linear element) and the acoustical space (considered as a perfectly linear system).

Figure 9: (a) Time representation of a Sine Sweep excitation signal ($\omega_1 = 2\pi 10$ rad/s and $\omega_2 = 2\pi 1000$ rad/s). (b) Corresponding Magnitude spectrum.

Figure 10: (a) Time representation of the inverse filter corresponding to the SineSweep signal presented in figure 9. (b) Corresponding Magnitude spectrum.
Figure 11: (a) Impulse Response obtained in an anechoic room with a logarithmic SineSweep of 1 second characterized by $\omega_1 = 2\pi 10 \text{ rad/s}$ and $\omega_2 = 2\pi 22000 \text{ rad/s}$. (b) Zoom on this response showing the extraordinary precision of the achievable results.

Figure 12: Schematic Representation of the measurement system.

Figure 13: (a) Impulse response obtained in an anechoic room when the excitation signal has been preequalized (in this example, the Logarithmic SineSweep technique has been used). (b) Corresponding Magnitude and Phase Spectra.
Figure 14: Disposition of the measurement elements in the anechoic room.

Figure 15: Zoom on the impulse responses obtained in the anechoic room with different methods. (a) MLS (b) IRS (c) Time-Stretched Pulses (d) SineSweep.
Figure 16: Impulse responses obtained in the anechoic room with different methods when an intense impulsive noise is simultaneously present. (a) MLS (b) Time-Stretched Pulses (c) SineSweep. Notice that the amplitude scales are not identical.
Figure 17: Impulse responses obtained in the auditorium 604 of the Europe Amphitheater of the University of Liège (Belgium). (a) MLS (b) IRS (c) Time-Stretched Pulses (d) SineSweep.
Figure 18: Zoom on the impulse responses obtained in the auditorium 604 of the Europe Amphitheater of the University of Liège (Belgium). (a) MLS (b) IRS (c) Time-Stretched Pulses (d) SineSweep.