



RELIABILITY PREDICTION

- Assess whether reliability goals can be reached
- Identify potential design weaknesses
- Compare alternative designs
- Analyse life-cycle costs
- Plan logistic support strategies (ie, repairing resources, ...)
- Establish objectives for reliability tests

FAILURE RATE λ

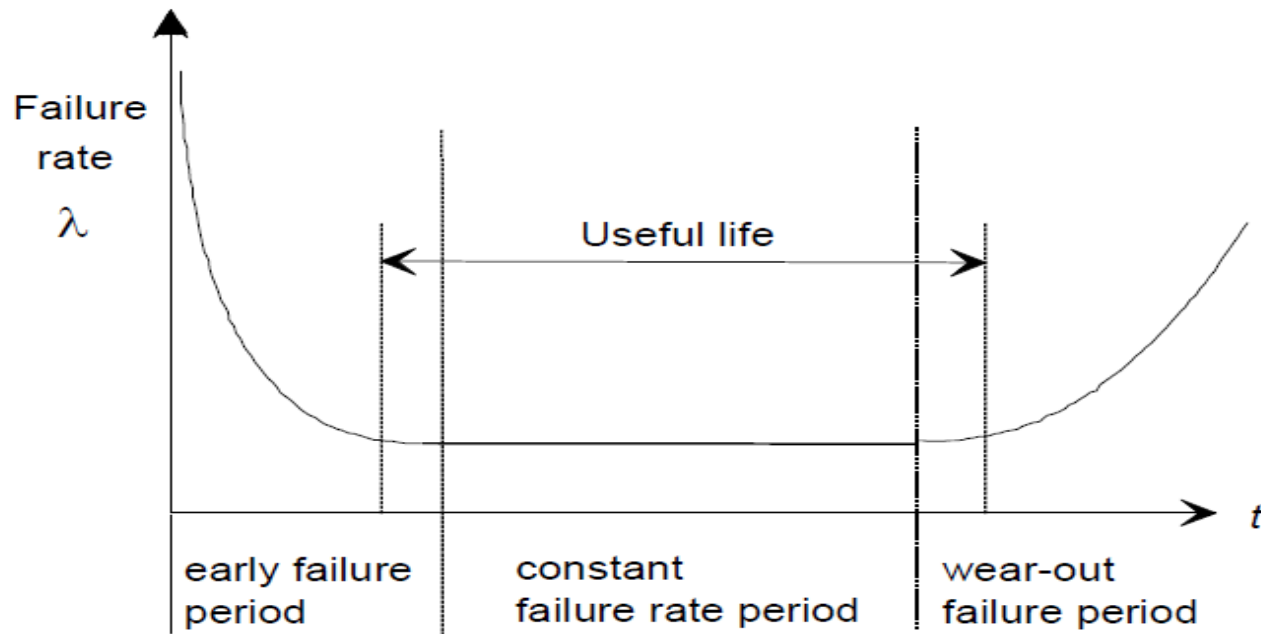


Figure 1.1 - The Bathtub Curve

λ : number of units failing per unit time



MTBF

Mean operating Time Between Failures

$$MTBF = \frac{1}{\lambda}$$

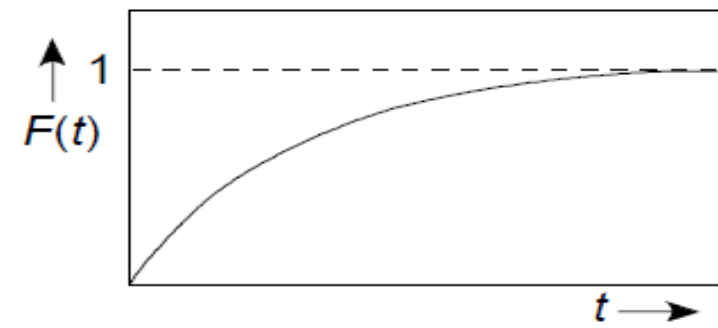
$$R(t) = e^{-\lambda t} = e^{\frac{-t}{MTBF}}$$

$$R(t) = e^{-1} = 0.37$$

- Probability of failure, distribution function

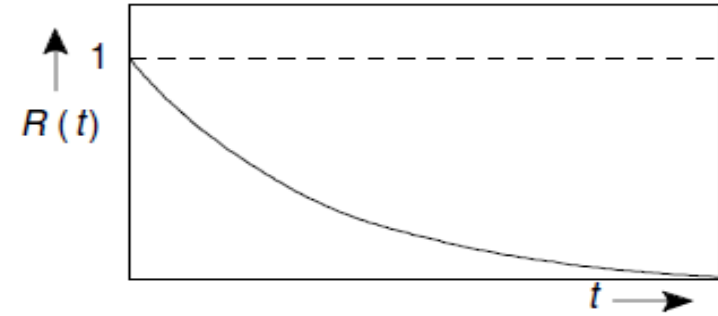
$$F(t) = 1 - \exp(-\lambda t), \quad \lambda > 0$$

Parameter λ (failure rate)



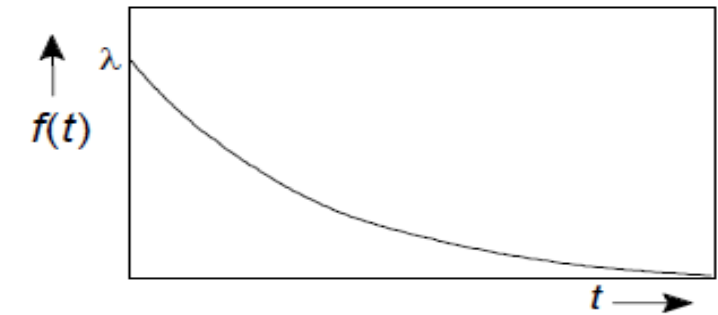
- Reliability

$$R(t) = \exp(-\lambda t), \quad \lambda > 0$$



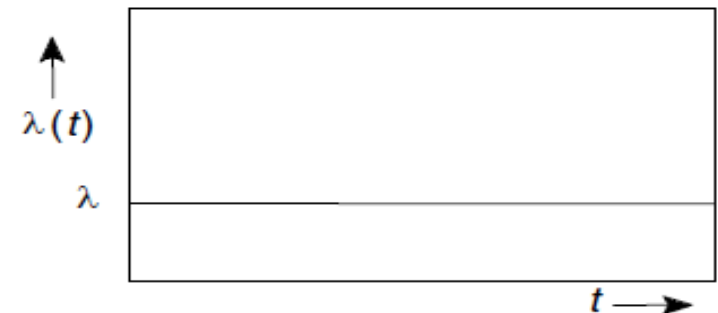
- Probability density function

$$f(t) = \frac{dF(t)}{dt} = \lambda \exp(-\lambda t)$$



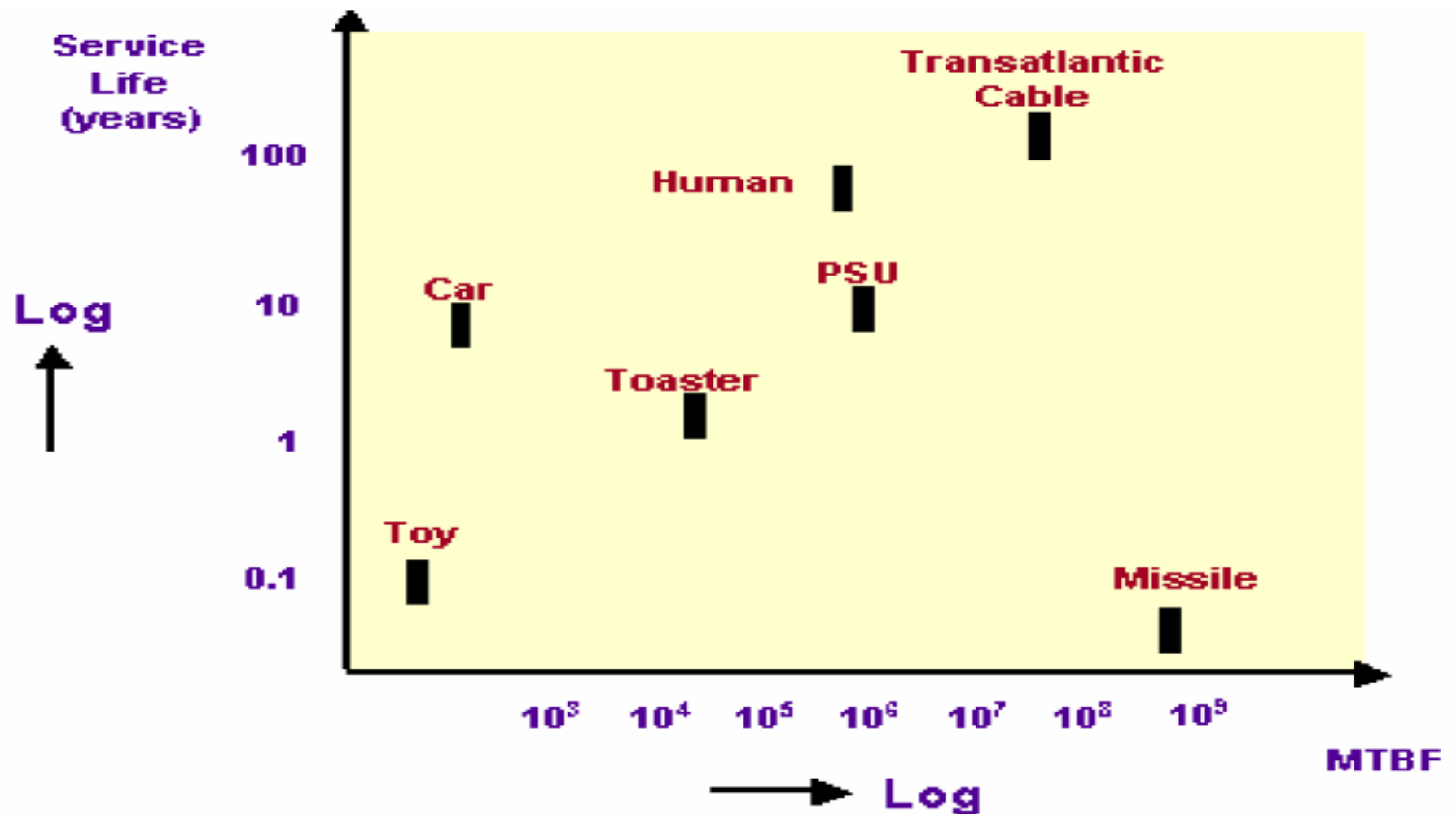
- Failure rate

$$\lambda(t) = \frac{f(t)}{1-F(t)} = \lambda = \text{const}$$



Service Life / Life Time

25 years old humans have an *MTBF* of about 800 years





Reliability Prediction Assumes:

- The design is perfect, the stresses known, everything is within ratings at all times, so that only random failures occur
- Every failure of every part will cause the equipment to fail.
 - The component reliability database is valid



Failure Rate Prediction

At Reference Conditions (Parts count)

$$\lambda_{S,i} = \sum_{i=1}^n (\lambda_{ref})_i ,$$

where

λ_{ref} is the failure rate under reference conditions;

n is the number of components



Failure Rate Prediction

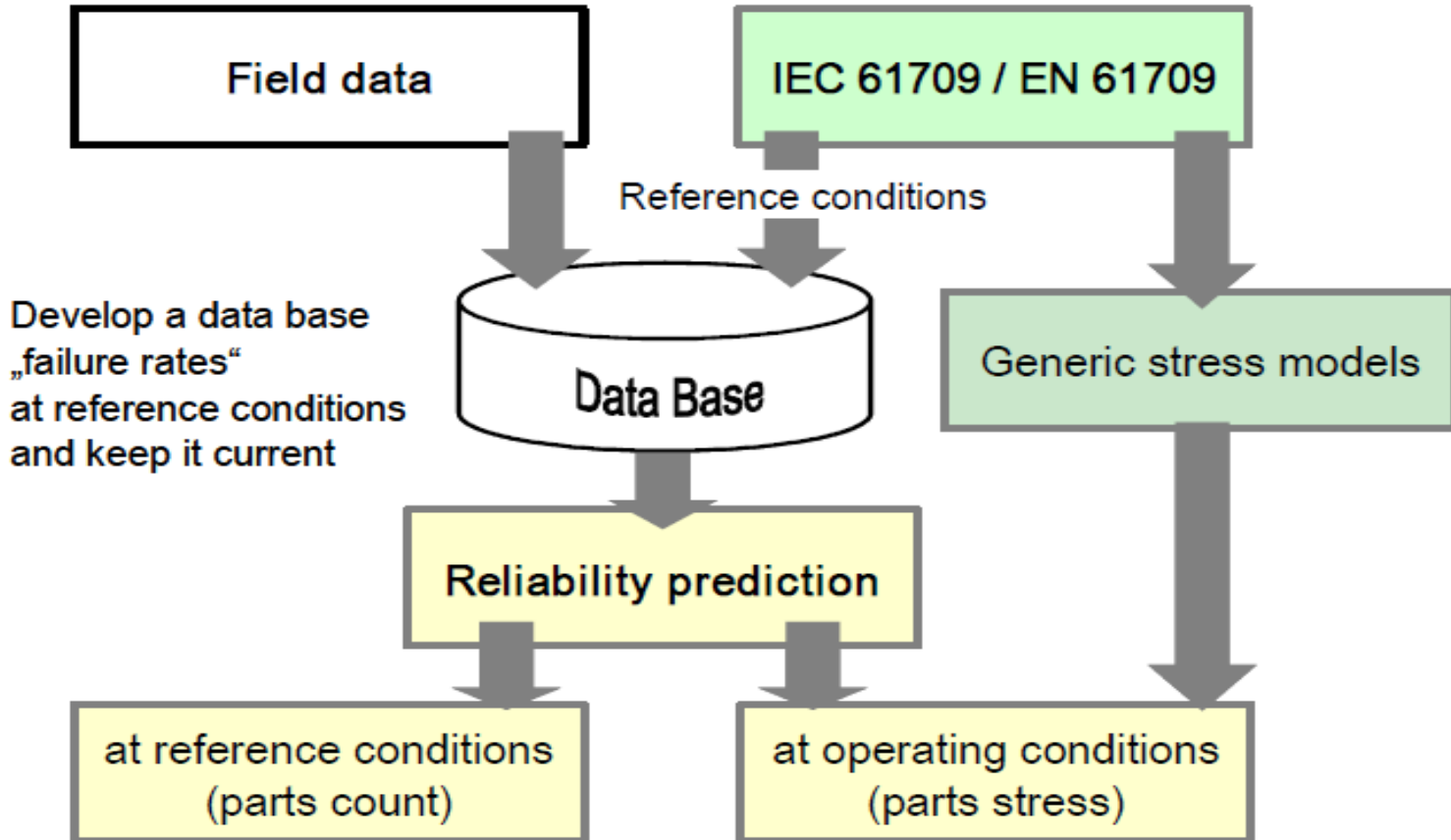
At Operating Conditions (Parts Stress)

$$\lambda = \sum_{i=1}^n \left(\lambda_{ref} \times \pi_U \times \pi_I \times \pi_T \right)_i$$

where

- λ_{ref} is the failure rate under reference conditions;
- π_U is the voltage dependence factor;
- π_I is the current dependence factor;
- π_T is the temperature dependence factor;
- n is the number of components

Prediction Methods



=> MTBF (250 kHours) @ Toperating (50°C)



Accelerated Life Testing

$$\text{Acceleration Factor } AF = \frac{tf_1}{tf_2} = \exp\left(\frac{E}{k}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)\right)$$

tf_1 = time to failure at temperature T_1

tf_2 = time to failure at temperature T_2

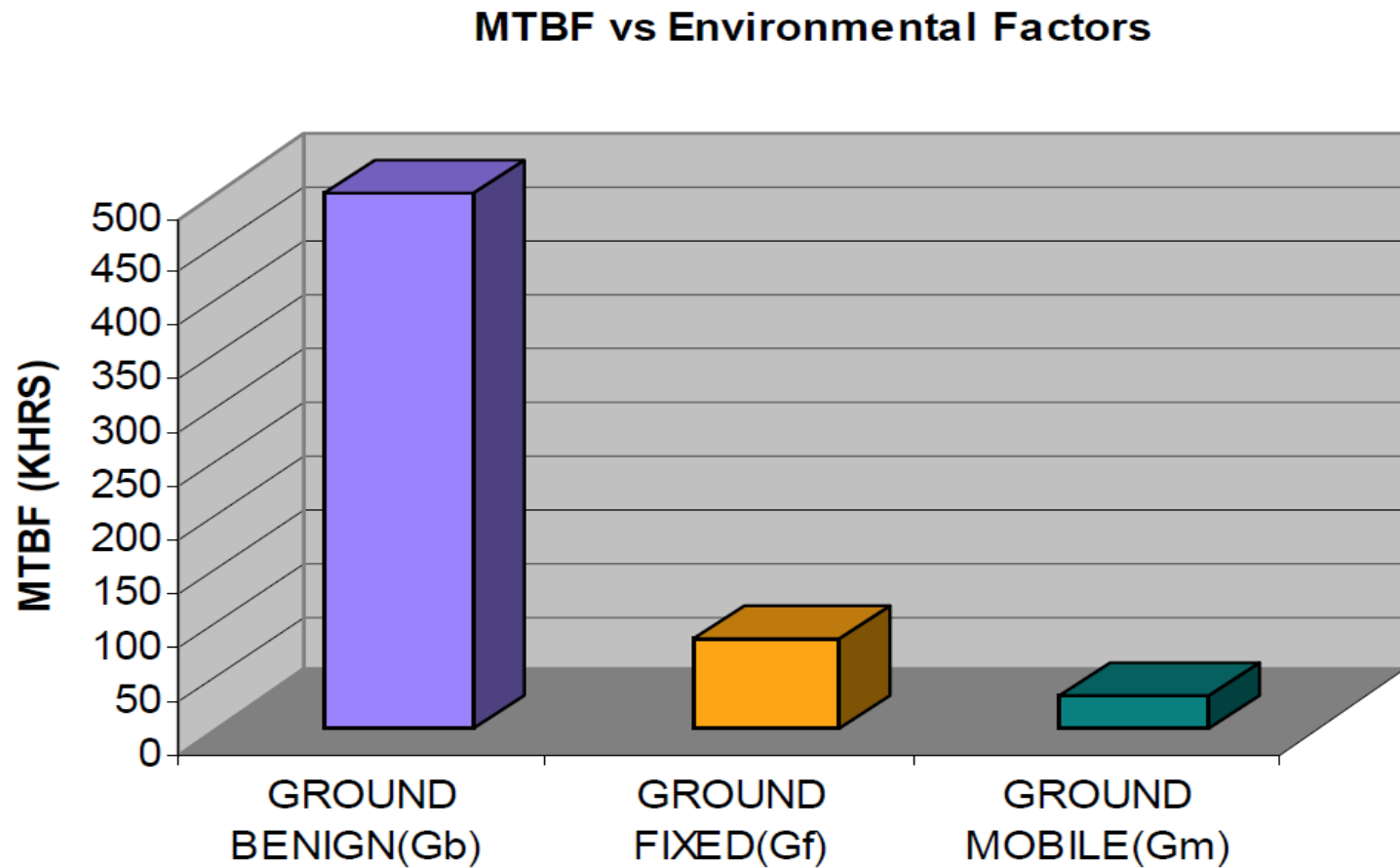
T_1, T_2 = temperature in degrees Kelvin ($^{\circ}\text{K}$)

E = activation energy per molecule (eV)

k = Boltzmann's constant (8.617×10^{-5} (eV/ $^{\circ}\text{K}$))

E from less than 0.3eV (gate oxide defect in a semiconductor)
to more than 1.1eV (contact electro-migration)

MTBF vs Environmental Factors



MTBF vs Power Load & T°

