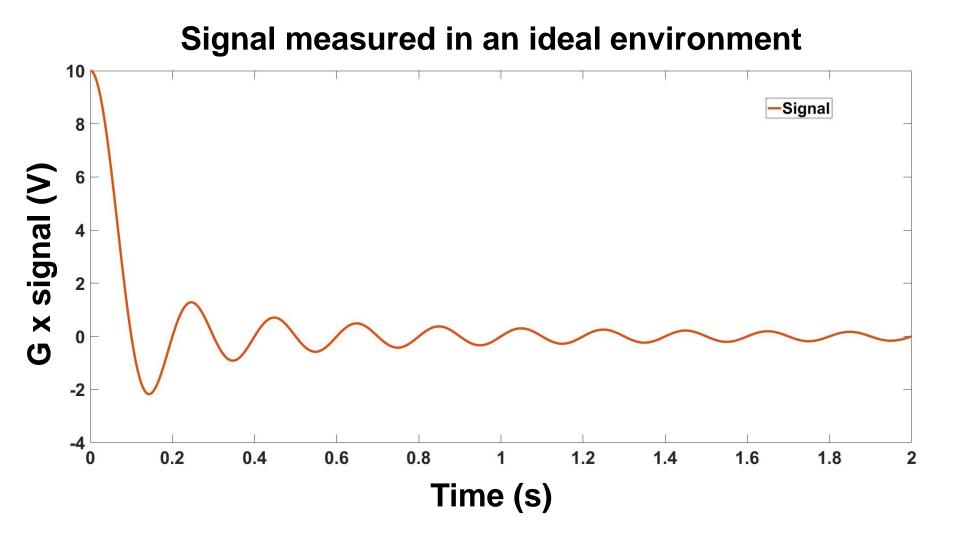
Powerline noise elimination MATLAB tutorial series (Part 2.2)

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Motivation

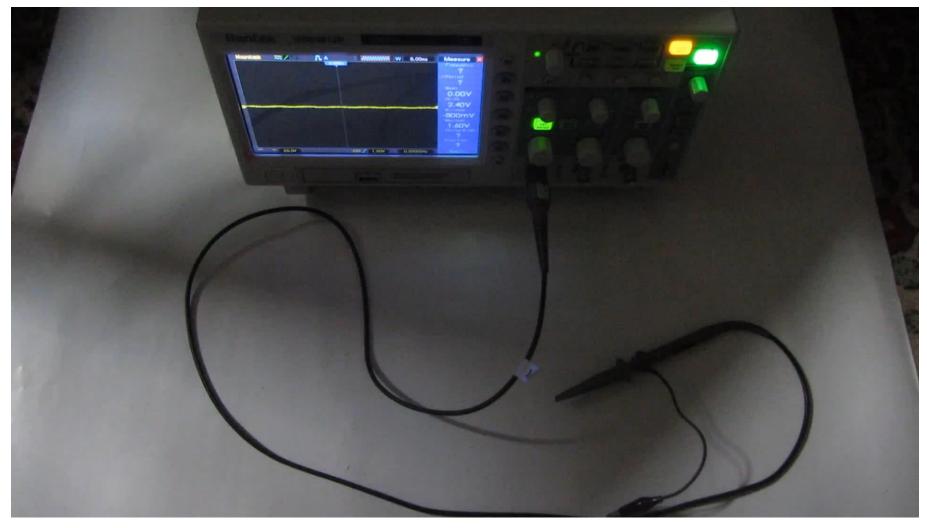


Motivation

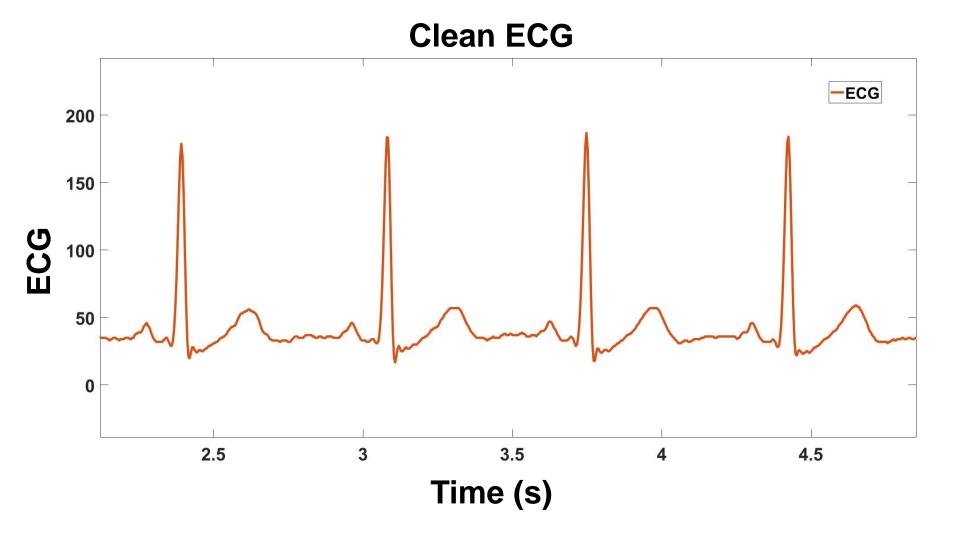
Signal measured in a real environment 10 Signal G x (signal + Noise) (V) Signal + Powerline noise 8 6 4 2 0 -2 -4 0 0.2 0.4 0.8 1.2 1.4 0.6 1.6 1.8 2 1 Time (s)

Human body as an antenna

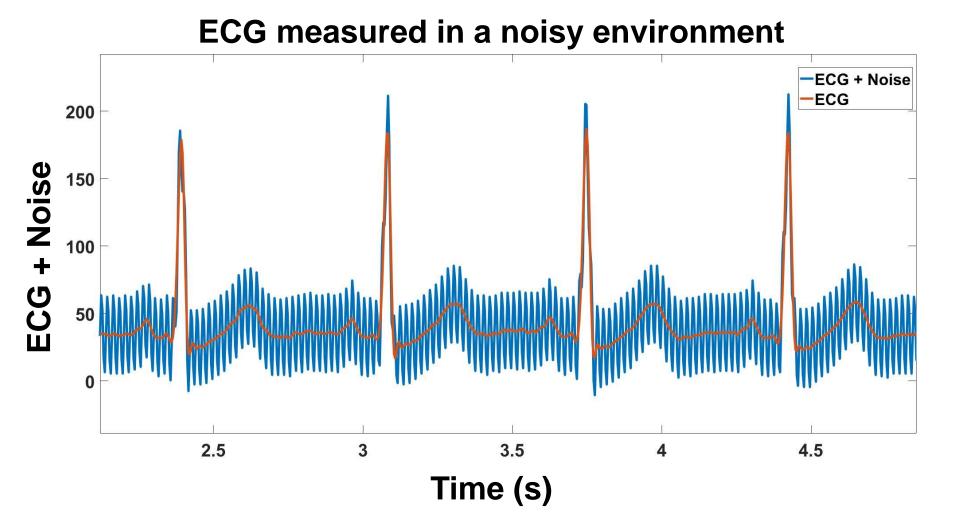
50Hz noise exists !



Electrocardiogram (ECG)



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- Step 1: plot the signal
 - \circ find the sampling period (Ts)
 - \circ find the ending time (Tmax)
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- Step 4: filter out undesired frequency components
 here we used Notch filter (i.e. Notching)
- Step 5: plot the results
 - Plot the original and filtered signals together

% Load ecg signal from .mat file load('TNS_2_1_2018_example1.mat','ecg')

% Load ecg signal from .mat file load('TNS_2_1_2018_example1.mat','ecg') % Fs is given Fs=250;

% Load ecg signal from .mat file load('TNS_2_1_2018_example1.mat','ecg') % Fs is given Fs=250; % Ts sampling period Ts=1/Fs; % Length of the signal N=length(ecg);

% Load ecg signal from .mat file load('TNS_2_1_2018_example1.mat','ecg') % Fs is given Fs=250; % Ts sampling period Ts=1/Fs;% Length of the signal N=length(ecg); % Ending time Tmax=(N-1)*Ts; % Time vector t=0:Ts:Tmax;

% Plot the original signal figure(1) plot(t,ecg) xlabel('Time (s)') title('ECG + noise')

% Compute fft ECG=fft(ecg);

% Compute fft
ECG=fft(ecg);
% Take abs and scale it
ECG2=abs(ECG/N);

% Compute fft ECG=fft(ecg); % Take abs and scale it ECG2=abs(ECG/N); % Pick the first half ECG1=ECG2(1:N/2+1);

% Compute fft ECG=fft(ecg); % Take abs and scale it ECG2=abs(ECG/N); % Pick the first half ECG1 = ECG2(1:N/2+1);% Multiply by 2 (except the DC part), to compenseate % the removed side from the spectrum. ECG1(2:end-1) = 2*ECG1(2:end-1);

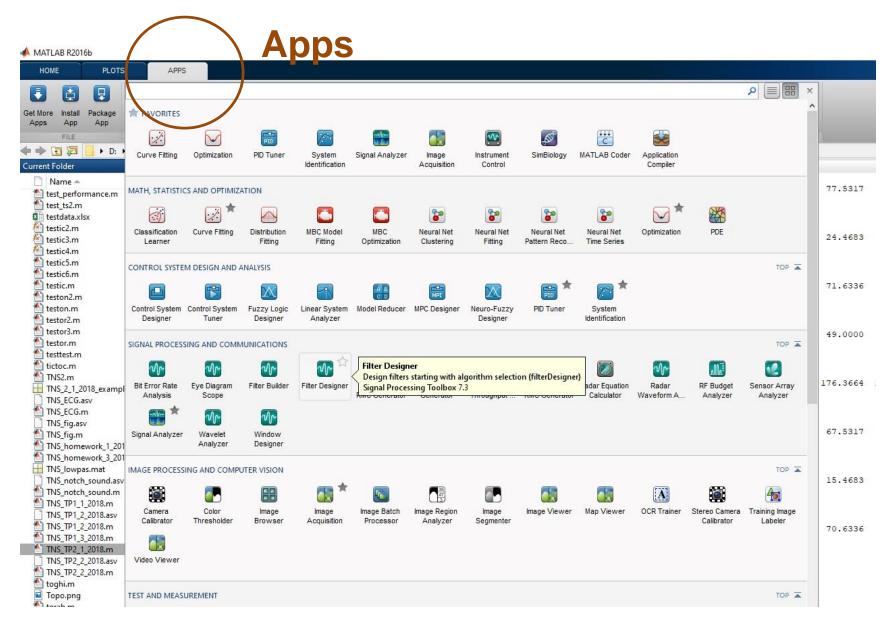
% Compute fft ECG=fft(ecg); % Take abs and scale it ECG2=abs(ECG/N); % Pick the first half ECG1 = ECG2(1:N/2+1);% Multiply by 2 (except the DC part), to compenseate % the removed side from the spectrum. ECG1(2:end-1) = 2*ECG1(2:end-1);% Frequency range $F = Fs^{*}(0:(N/2))/N;$

% Plot single-sided spectrum figure(2) plot(F,ECG1,'LineWidth',2.5) title('Single-Sided Amplitude Spectrum') xlabel('f (Hz)');

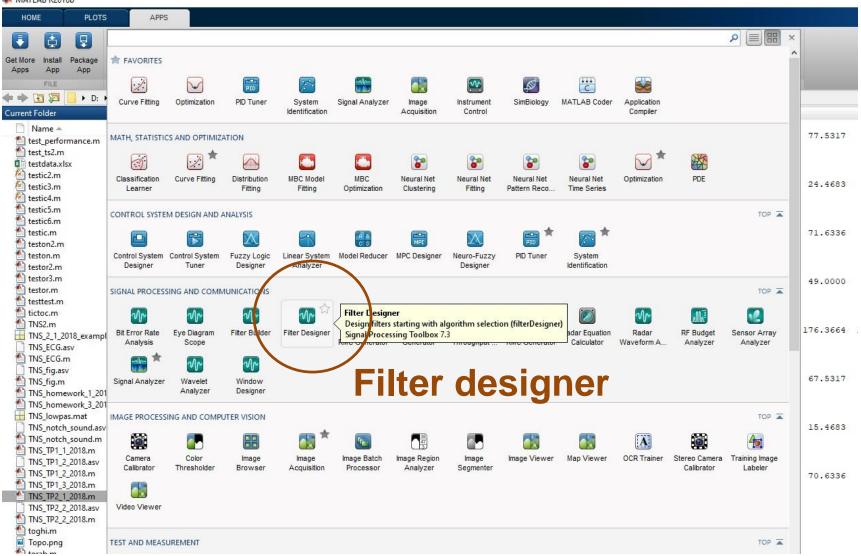
Step 3: identify the noise frequencies

Just take a look to the single-sided magnitude spectrum and you will see

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A MATLAB R2016b



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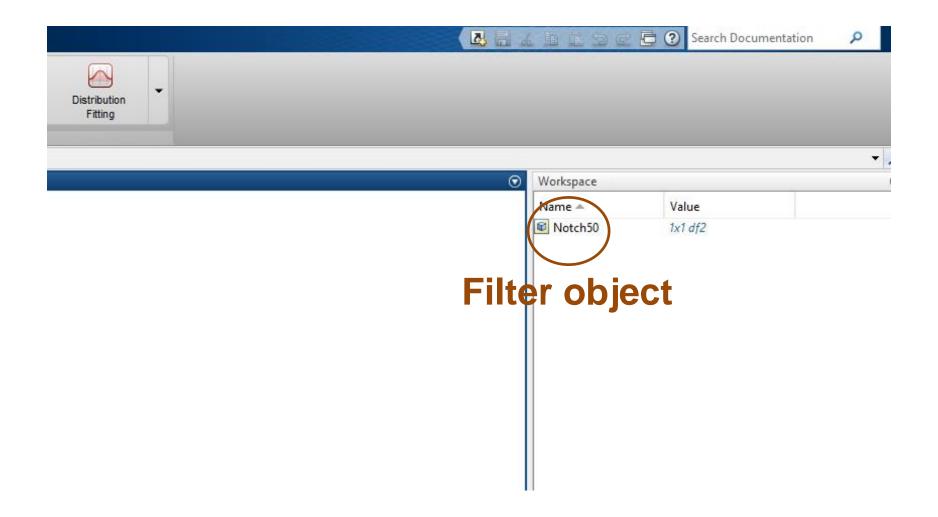
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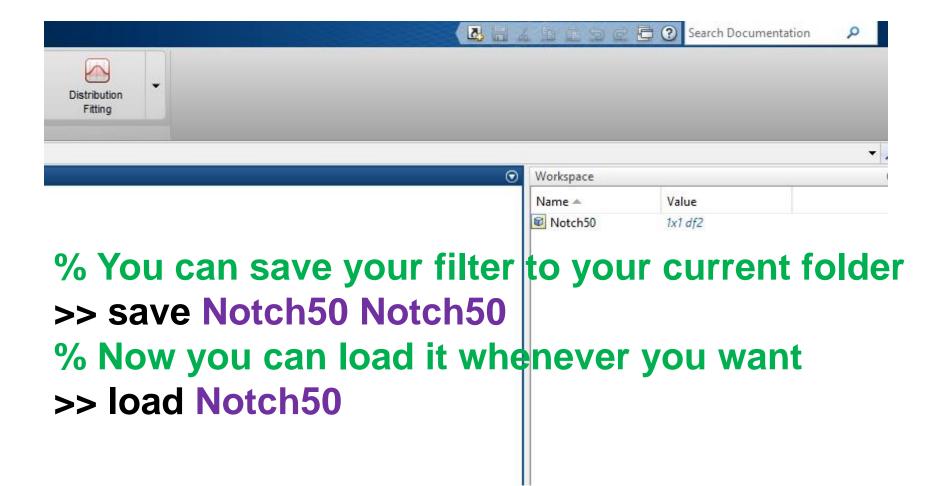
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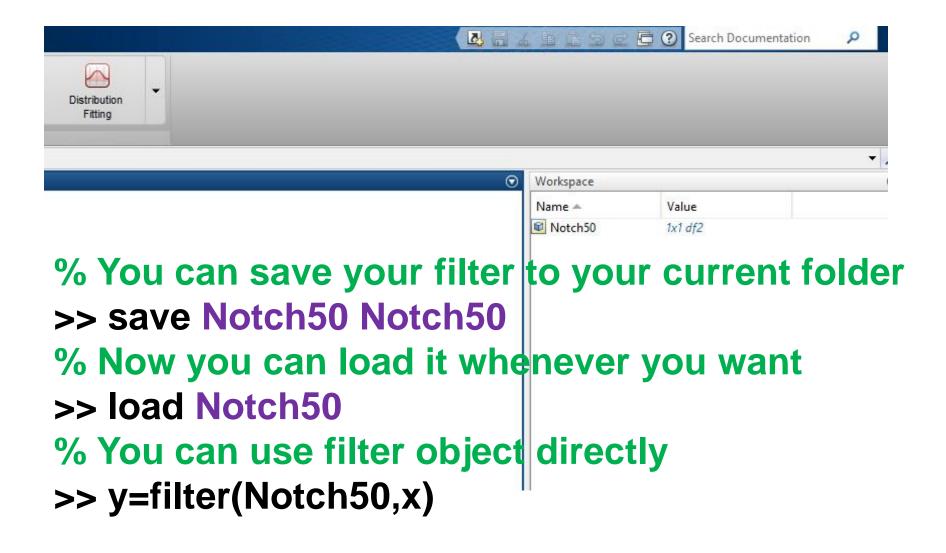
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Step 4: filter out undesired frequency components

% load the filter object load Notch50; % removing the noise pure_ecg=filter(Notch50,ecg);

Step 5: plot the results

```
figure(3)
plot(t,pure ecg,'LineWidth',2); title('without noise')
xlabel('time (s)')
ylabel('amplitude')
% Zoom in
figure(4)
plot(t(500:length(t)/6),ecg(500:length(t)/6),...
'LineWidth', 2.5); title('Noisy and without noise')
xlabel('time')
ylabel('amplitude')
hold on
plot(t(500:length(t)/6), pure ecg(500:length(t)/6),...
'LineWidth',2.5)
```

Open filter visualization tool

MATLAB: fvtool(b,a) or fvetool(object) or

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Useful links

- <u>https://www.youtube.com/watch?v=utrb6DN-Pqc</u>
- <u>https://www.youtube.com/watch?v=aZ9fnLzPIWo</u>
- <u>https://nl.mathworks.com/help/signal/ug/getting-</u> <u>started-with-filter-designer.html</u>