

# Semantic Data

## Chapter 6 : The Web Ontology Language OWL

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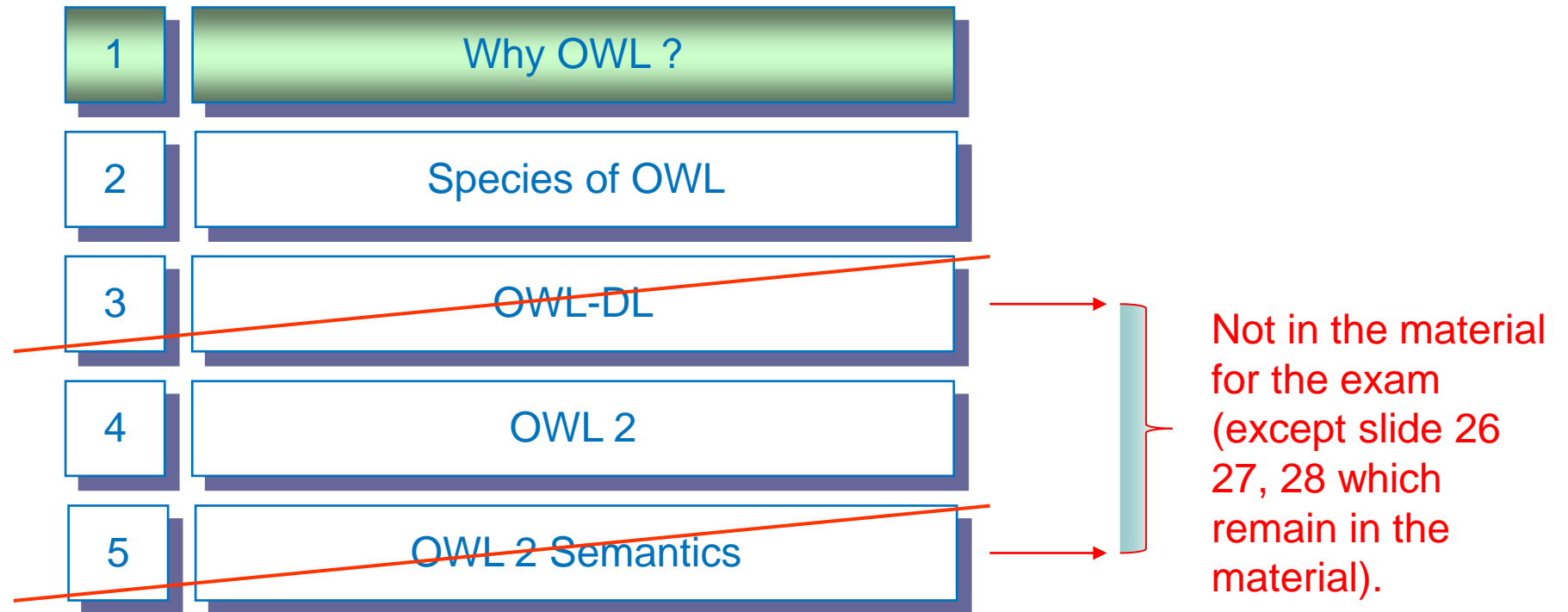
# Sources and recommended readings

- There are no additional required references for this chapter for the theory.  
Some sections have been taken out of the material for the exam.

The [Manchester syntax](#) is not covered in theory but is useful in practice (in Protégé). Students are expected to acquire the knowledge they need for the project.

- Sources and useful additional readings :
  - The presentation of OWL DL is based on the [OWL guide 2004](#).
  - The presentation of OWL 2 is based on the [OLW 2 primer](#) and the [OWL 2 new features and rationale](#).
  - *Web Data Management (Abiteboul et al. 2011)* covers succinctly the link between DL and OWL.
  - *An introduction to description logic (Baader et al. 2017), chapter 8*, covers the mappings between OWL and description logics.
- University courses having partially inspired ideas and examples for this chapter :
  - *Description Logics part 1 Languages, I. Horrocks, Oxford University.*
  - *Apprentissage symbolique et web sémantique, B. Amman, Université Pierre et Marie Curie, Paris.*
  - *OWL 2 Web Ontology Language Revised, S. Wandelt, Humboldt-Universität zu Berlin.*
  - *Semantic Web Technologies, H. Paulheim, Universität Mannheim.*

# Agenda

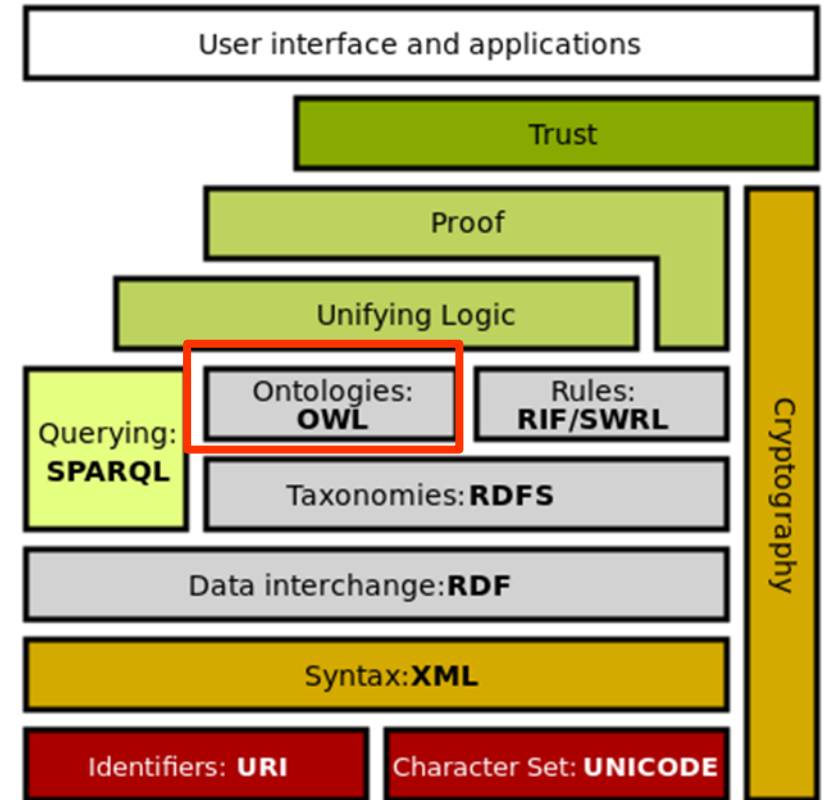
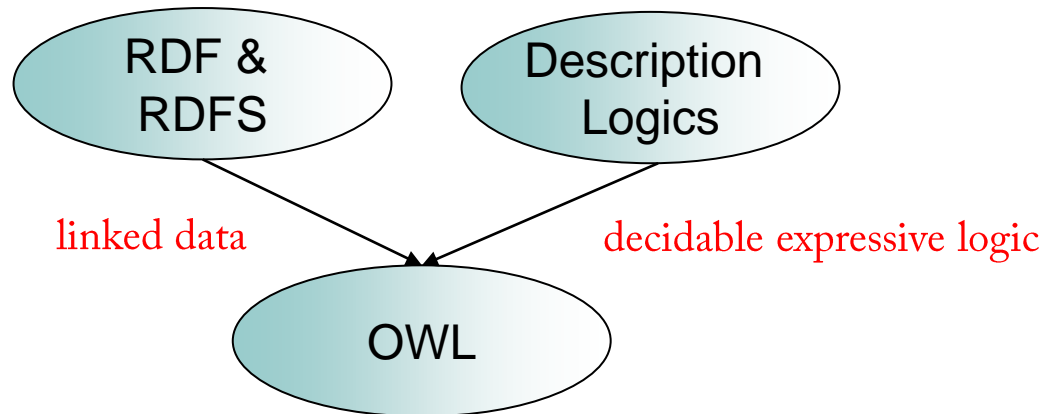


# OWL in the W3C standards stack

RDFS supports only lightweight ontologies (cf. chapter 4).

OWL (Web Ontology Language) is a language for building **full** Web ontologies with model-theoretic semantics.

- OWL uses RDF and RDFS to manipulate linked data.
- OWL (in its main variant) uses description logics to support logical inferences.
- This “merging of two worlds” raises a few difficulties.



*The semantic web stack of standards*

# Why not just build OWL as an extension of RDFS ?

- ❑ **RDFS** modeling primitives are sources of **unwanted complexity**.
  - Constructions such as *rdfs:Class* and *rdf:Property* are very powerful :  
A class may be an instance of itself; a property may be applied to itself.
  - Combined with OWL's language extensions, this may create undecidability. W3C has given a **choice** :
  
- ❑ **OWL-Full** : total freedom to use RDF, for those wanting to use that freedom.  
But : not reasoner exist for all features; **the entailment problem in OWL-Full is undecidable** !
  
- ❑ **OWL-DL** : The model-theoretic semantics of description logics apply; **reasoners exist**.  
But: RDF is restricted to what is needed to express OWL DL concepts and axioms.  
*owl:Class* is a proper subclass of *rdfs:Class*. A class cannot be also an instance. Other restrictions apply.

# Agenda

- 1 Why OWL ?
- 2 Species of OWL
- 3 OWL-DL
- 4 OWL 2
- 5 OWL 2 Semantics

# Species of OWL

- OWL 1 (2004): three increasingly expressive sublanguages for distinct uses:
  - **OWL Full**: maximum expressiveness; syntactic freedom of RDF (e.g., classes can also be instances).  
No reasoner supports all features of OWL Full.
  - **OWL DL**: maximum description logic expressivity while guaranteeing completeness and decidability.  
Every entailment can be computed by a reasoner.
  - **OWL Lite**: classification hierarchy and simple constraints. Quick migration path for thesauri and taxonomies.
- All these languages support upward compatibility :
  - Every legal *OWL Lite* ontology is a legal *OWL DL* ontology.  
Every valid *OWL Lite* conclusion is a valid *OWL DL* conclusion.
  - Every legal *OWL DL* ontology is a legal *OWL Full* ontology.  
Every valid *OWL DL* conclusion is a valid *OWL Full* conclusion.
- OWL 2 (2009), evolution of OWL 1.

# Mapping with description logics

Reminder :  $\mathcal{S}$  denotes logic  $\mathcal{ALC}$  extended with transitive roles :

- $\mathcal{S} = \mathcal{ALCR}^+$  (cf. chapter 4 for a description of the naming scheme).

OWL  $\leftrightarrow$  description logics correspondences :

- **OWL Lite** :  $\leftrightarrow$   $\mathcal{SHIF}$  (role hierarchies, inverse roles, functions)
- **OWL – DL** :  $\leftrightarrow$   $\mathcal{SHOIN}(\mathcal{D})$  (role hierarchies, nominals, inverse roles, number restrictions, data types)
- **OWL – Full** :  $\leftrightarrow$  **undecidable**
- **OWL 2** :  $\leftrightarrow$   $\mathcal{SROIQ}(\mathcal{D})$  (complex roles and role axioms, nominals, inverse roles, qualified number restrictions, data types)

OWL 2 is the most expressive OWL language where inferencing is still decidable.

However, many large ontologies are still in OWL1.



# OLW Syntaxes

Examples of the first 5 syntaxes can be found in the [OLW2 Primer](#)

❑ RDF/XML syntax :

- Still the only *normative* syntax.

❑ Turtle syntax : straightforward Turtle version of the RDF/XML Syntax.

We will only cover Turtle

❑ Functional Style syntax :

- Prefix-syntax, given as formal grammar; clean, adjustable, modifiable, easily parsable; used in W3C Specs.

❑ Manchester syntax: user-friendly syntax, used in Protégé.

❑ OWL/XML syntax :

- Notational variant of Functional Style Syntax. Does not use RDF triples, but XML tree structure.

❑ Graphical syntax based on UML conventions.

❑ **Probably too many syntaxes : complex design choices, multiplication of conversions...**

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- 1 Why OWL ?
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- 4 OWL2
- 5 OWL2 Semantics

# Namespaces and prefixes

- A typical OWL ontology starts with namespace declarations (as RDF).

- The OWL namespace is defined by :

*PREFIX owl: <http://www.w3.org/2002/07/owl#> .*

- Other namespaces seen in previous chapters will be reused, among which :

*PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .*

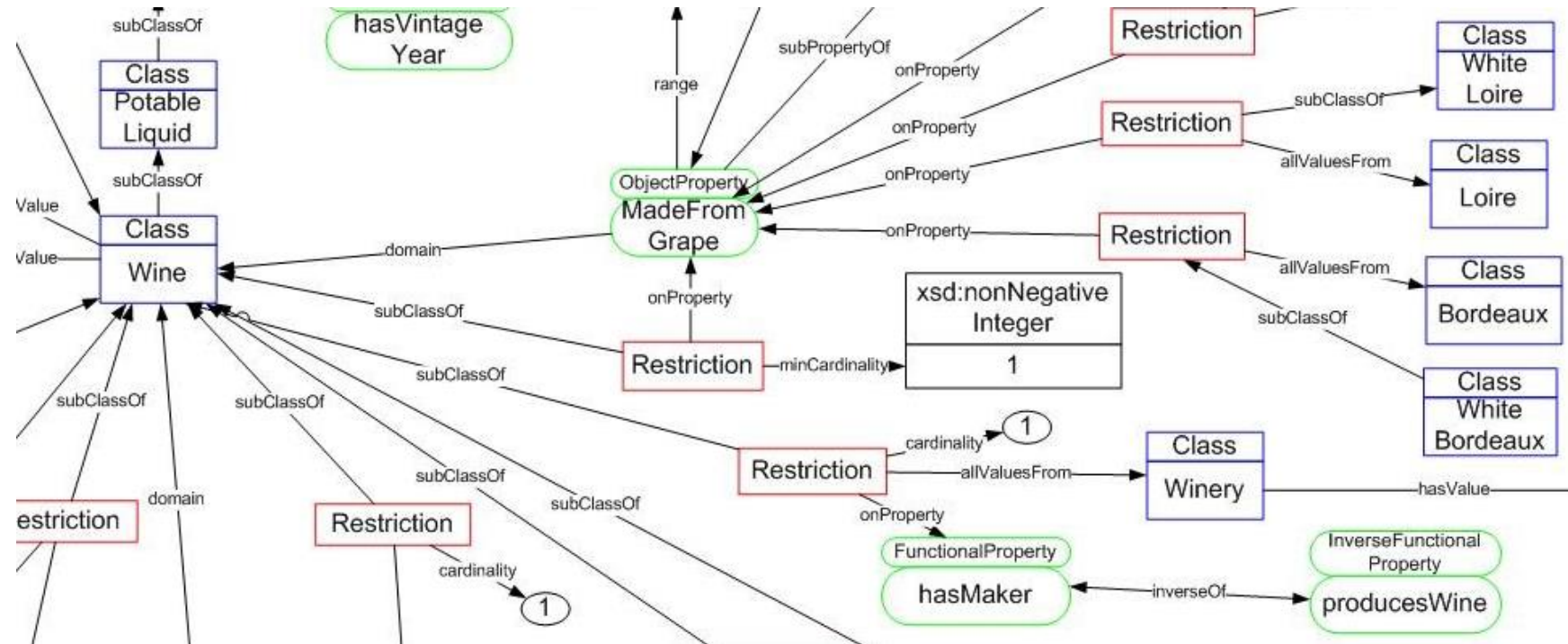
*PREFIX rdfs: <http://www.w3.org/2000/01/rdf-schema#> .*

- Examples from the wine ontology (downloadable) use the following prefixes :

*PREFIX vin: <http://www.w3.org/TR/2003/PR-owl-guide-20031209/wine#> .*

*PREFIX food: <http://www.w3.org/TR/2003/PR-owl-guide-20031209/food#> .*

# Example ontology : the Wine ontology



A wine is a potable liquid produced by one maker of type winery, and made from at least one type of grape...

(Source for the ontology: [wine](#) and [food](#))

Source for image: Owl language guide: <http://www.w3.org/TR/owl-guide.rdf>, using VisioOWL)

# Expressing DL in OWL, an example

## □ DL axioms :

$\text{Wine} \subseteq \text{PotableLiquid} \sqcap \forall \text{hasMaker.Winery}$   
 $\text{ChateauChevalBlanc} : \text{Winery}$

## □ In OWL :

`vin:PotableLiquid a owl:Class .`

`vin:Winery a owl:Class .`

`vin:Wine a owl:Class ;`

`rdfs:subClassOf vin:PotableLiquid ;`

`rdfs:subClassOf [ a owl:Restriction ;`

`owl:onProperty vin:hasMaker ;`

`owl:allValuesFrom vin:Winery ] .`

`vin:ChateauChevalBlanc a vin:Winery .`

## □ A class may be :

- Identified by name (an URI);
- Anonymous (RDF `[]` blank node notation).

## □ Syntactic constructs :

- `rdf:type (a)` : to type resources / declare instances.
- `rdfs:subClassOf` : specialization hierarchy.
- `owl:Class` : the type `Class`.

# Thing and Nothing

- **Owl:Thing** is the universal concept,  $\top$ .
  - Every individual in the interpretation domain is a member of the class **owl:Thing**.
  - Each user-defined class is implicitly a subclass of **owl:Thing**.
  
- **Owl:Nothing** is the inconsistent concept,  $\perp$ .
  - No individual of the interpretation domain belongs to **Owl:Nothing**.

# Types of class restrictions

An OWL class can be defined by :

1. Constraints on properties of the instances (intensional definition);
2. Enumeration of its instances (extensional definition);
3. Set relationships on the extensions of other classes.

# 1. Constraints on the properties of the instances

## □ Structure:

```
<class> rdfs:subClassOf <restriction>  
<restriction> ::= [a owl:Restriction ;  
                   owl:onProperty <property> ;  
                   <restriction name> <restriction argument>]
```

## □ Example :

```
vin:Burgundy a owl:Class ;  
             rdfs:subClassOf [ a owl:Restriction ;  
                               owl:onProperty vin:hasSugar ;  
                               owl:hasValue vin:Dry ] .
```

### ■ In DL :

Burgundy  $\sqsubseteq$   $\exists$ hasSugar.{Dry}



# Constraints on the properties of the instances ./.

Constraint	OWL	DL
Property value type restrictions		
<i>Existential restriction</i>	[owl:onProperty r ; owl:someValuesFrom C]	$\exists r.C$
<i>Universal restriction</i>	[owl:onProperty r ; owl:allValuesFrom C]	$\forall r.C$
Cardinality restrictions		
<i>Minimum cardinality</i>	[owl:onProperty r ; owl:minCardinality n]	$\leq n r^{(*)}$
<i>Maximum cardinality</i>	[owl:onProperty r ; owl:maxCardinality n]	$\geq n r^{(*)}$
Property value restriction	[owl:onProperty r ; owl:hasValue v]	$\exists r.\{v\}$

(\*): n is written in RDF format, e.g. "1"^^xsd

## 2. Enumerated classes

- A class can be specified via a direct enumeration using `owl:oneOf`:
  - This completely specifies the class extension : no other individuals can be declared to belong to the class.

```
vin:WineColor a owl:Class ;  
            owl:oneOf ( vin:Red vin:Rose vin:White) ;  
            rdfs:subClassOf vin:WineDescriptor .
```

- In DL ( $\mathcal{O}$ ) : the set (or “one-of”) constructor :

`WineColor  $\equiv$  {Red, Rose, White}`

### 3. Class definitions using set relationships

Class definitions may use inclusion, equivalence, disjoint relationships.

- Inclusion : `rdfs:subClassOf`. In DL : a GCI axiom :  $C \subseteq D$ .
- Equivalence : `owl:equivalentClass`. In DL : an equivalence axiom :  $C \equiv D$ .
- Disjoint classes : `owl:disjointWith`. In DL :  $A \sqcap B \subseteq \perp$ .

Example :

```
food:Fowl a owl:Class ;  
    rdfs:subClassOf food:EdibleThing ;  
    owl:disjointWith food:Fruit ;  
    owl:equivalentClass food:Poultry .
```

### 3. Class definitions using set relationships ./.

□ Complex class definitions may use the Boolean set operators :

- DL:  $\sqcap, \sqcup, \neg$  .
- OWL : `owl:intersectionOf`, `owl:unionOf`, `owl:complementOf` .

□ Structure :

[`rdf:type owl :Class`; `<set operator>` (`<class>` ... `<class>`)]

□ Example :

```
vin:WhiteWine owl:equivalentClass
  [a owl:Class ;
   owl:intersectionOf ( vin:Wine [ a owl:Restriction ; owl:onProperty vin:hasColor ;
                                   owl:hasValue vin:White] ) ] .
```

DL:  $WhiteWine \equiv Wine \sqcap \exists hasColor.\{White\}$

# A larger example

- Let us revise the definition of *Wine* to cover the following information :

*“A wine is a potable liquid made from at least one grape; its maker must be a winery; it must be located in one region”.*

```
vin:Wine a owl:Class ;
```

```
  rdfs:subClassOf food:PotableLiquid ,
```

```
  [ a owl:Restriction ; owl:onProperty vin:locatedIn ; owl:someValuesFrom vin:Region ] ,
```

```
  [ a owl:Restriction ; owl:onProperty vin:hasMaker ; owl:allValuesFrom vin:Winery ] ,
```

```
  [ a owl:Restriction ; owl:onProperty vin:madeFromGrape ; owl:minCardinality  
    "1"^^xsd:nonNegativeInteger] .
```

- In DL :

- $Wine \subseteq PotableLiquid \sqcap \exists locatedIn.Region \sqcap \forall hasMaker.Winery \sqcap \geq 1 madeFromGrape$

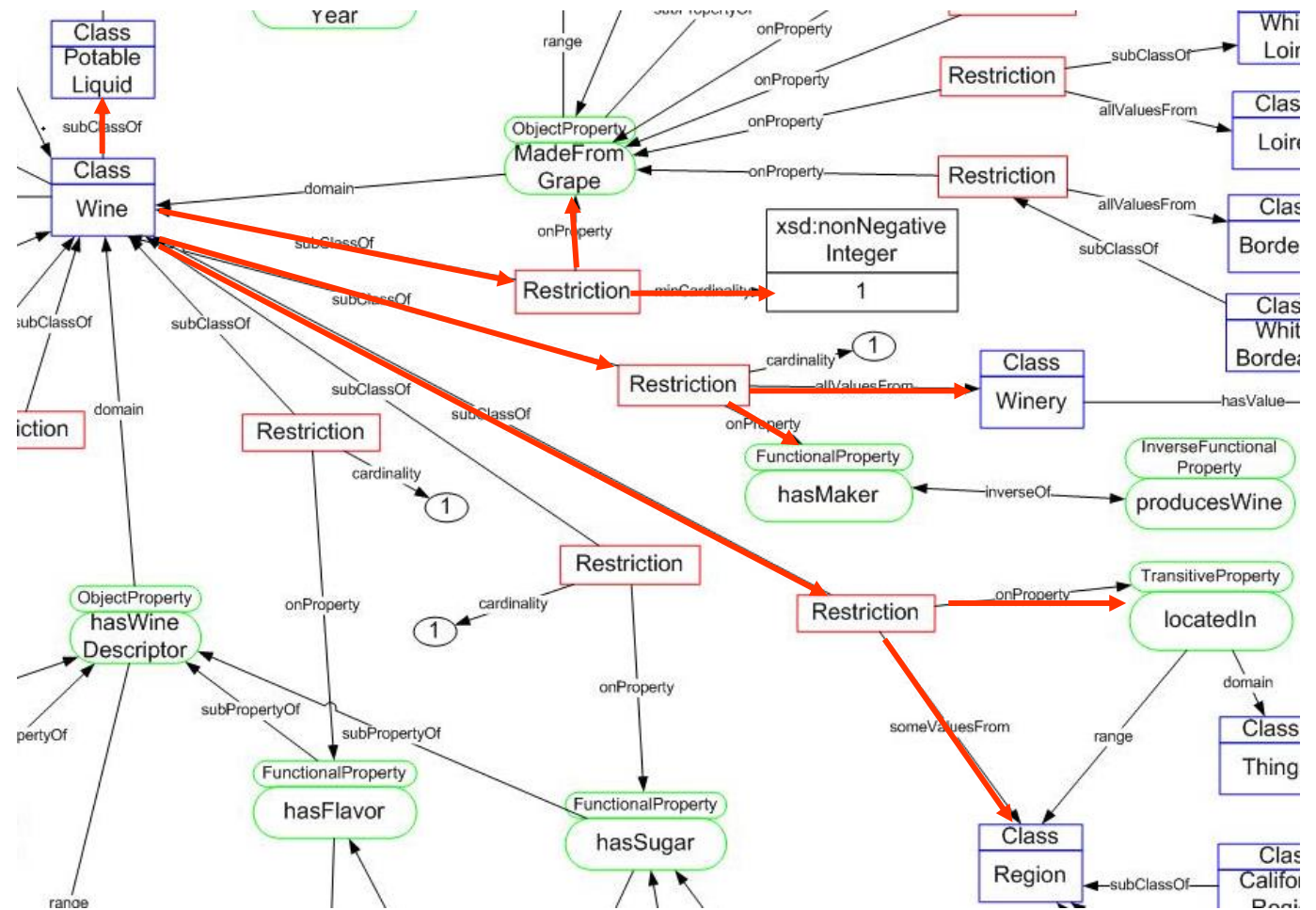
# Graph-based visualisation

*vin:Wine* *rdf:type* *owl:Class* ;  
*rdfs:subClassOf* *food:PotableLiquid* ,

[ *rdf:type* *owl:Restriction* ;  
*owl:onProperty* *vin:locatedIn* ;  
*owl:someValuesFrom* *vin:Region* ] ,

[ *rdf:type* *owl:Restriction* ;  
*owl:onProperty* *vin:hasMaker* ;  
*owl:allValuesFrom* *vin:Winery* ] ,

[ *rdf:type* *owl:Restriction* ;  
*owl:onProperty* *vin:madeFromGrape*  
; *owl:minCardinality*  
"1"^^*xsd:nonNegativeInteger* ] .



# Properties

Two types of properties are distinguished:

- **Object properties** : type `owl:ObjectProperty`.
  - Express relations between instances of two classes.
  
- **Datatype or value properties** : type `owl:DatatypeProperty`.
  - Express relations between instances of classes and datatypes (RDF or XML Schema types).

Both are subclasses of `rdf:Property`.

# OWL property characteristics

- RDFS property **hierarchies**, **domain** and **range** are still usable.

```
vin:madeFromGrape a owl:ObjectProperty ;  
  rdfs:subPropertyOf food:madeFromFruit ;  
  rdfs:domain vin:Wine ;  
  rdfs:range vin:WineGrape .
```

```
vin:FormanCabernetSauvignon vin:madeFromGrape vin:CabernetSauvignonGrape .
```

- **Property hierarchies** in DL ( $\mathcal{H}$ ) : a role inclusion axiom:  $\text{madeFromGrape} \sqsubseteq \text{madeFromFruit}$
- **Domain** in DL :  $\exists \text{madeFromGrape} . \top \sqsubseteq \text{Wine}$
- **Range** in DL :  $\top \sqsubseteq \forall \text{madeFromGrape} . \text{WineGrape}$

We can, among others, infer from the example above that **FormanCabernetSauvignon** is a wine.

- As OWL uses DL, the domain or range can be a complex class (in contrast with RDFS) :
  - Domain :  $\exists \text{childOf} . \top \sqsubseteq \text{Father} \sqcup \text{Mother}$



# Property axioms

- Property axioms (transitive, symmetric ...) are defined by making the property an instance of the appropriate built-in OWL property class :

- `vin:locatedIn` a `owl:TransitiveProperty` .      In DL : *Trans(locatedIn)*

The range of a transitive property must be subsumed by its domain.

- `vin:adjacentRegion` a `owl:SymmetricProperty` .      In DL : *adjacentRegion ≡ adjacentRegion<sup>-</sup>*

The domain and range of a symmetric property must be the same.

- `vin:hasMaker` a `owl:FunctionalProperty` .      In DL :  $\top \sqsubseteq (\leq 1 \text{ hasMaker})$

- Inverse properties are defined by using the built-in *owl:inverseOf* property :

- *vin:madeFromGrape* *owl:inverseOf* *vin:madeIntoWine* .      In DL : *madeFromGrape ≡ madeIntoWine<sup>-</sup>*

# Revisiting the example from chapter 1

`:country a rdf:class .`  
`:city a rdf:class .`  
`:capitalOf rdfs:subPropertyOf :locatedIn .`  
`:capitalOf rdfs:domain :city .`  
`:capitalOf rdfs:range :country .`  
`:locatedIn a :rdf:property .`



*“Madrid is the capital of Spain”*

`:Madrid :capitalOf :Spain .`

*(example after Paulheim,  
Semantic Web Technologies)*



Status with RDFS :

✓ Madrid is a city.

✓ Spain is a country.

✓ Madrid is located in Spain.

✗ Barcelona is not the capital of Spain.

✗ Madrid is not the capital of France.

✗ Madrid is not a country.

□ How can we do it with DL and OWL ?

# Revisiting the example from chapter 1 ./.

DL

OWL

- Madrid is not the capital of France

$\text{City} \sqsubseteq \leq 1 \text{ capitalOf.Country}$

`:capitalOf a owl:FunctionalProperty .`

`:Madrid :capitalOf :Spain .`

`:Spain owl:differentFrom :France .`

`:Madrid :capitalOf :France . => inconsistent ontology`

- Barcelona is not the capital of Spain

$\text{Country} \sqsubseteq =1 \text{ hasCapital.City}$

(abbreviation for  $\geq 1 \text{ hasCapital.City} \sqcap \leq 1 \text{ hasCapital.City}$ )

`:Country a owl:Class ;  
rdfs:subClassOf [a owl:Restriction ; owl:onProperty :hasCapital ;  
owl:qualifiedCardinality "1"^^xsd:nonNegativeInteger ; owl:onClass :City ] .`

`:Spain hasCapital :Madrid.`

`:Madrid owl:differentFrom :Barcelona .`

`:Spain :hasCapital :Barcelona . => inconsistent ontology`

- Madrid is not a country.

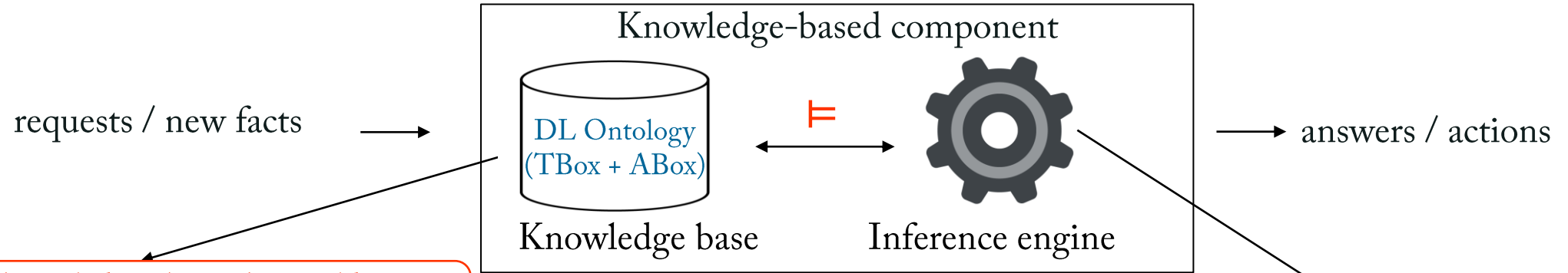
$\text{City} \sqcap \text{Country} \sqsubseteq \perp$

`:Madrid a :City .`

`:City owl:disjointWith :Country .`

`:Madrid a :Country => inconsistent ontology`

# Updated framework of reference for semantic applications



How to express knowledge about the world?  
Use description logics

In what kind of databases shall we store this type of data / knowledge ?

Which formalism(s) to represent and access the meaning of web resources?  
Semantic web standards (RDF(S) and OWL).

How to perform deductions?  
Use entailment

# Ontology management

- **Meta-information** about the ontology itself can be specified:
  - **rdfs:label** provides a human-readable version of the ontology name.
  - **rdfs:comment** provides the obviously needed ability to comment.
  - **owl:priorVersion** provides information that may be used for version control.
  - **owl:imports** allows to import other ontologies, bringing their full set of assertions into the current ontology.
- **Class declarations** are also part of ontology management. All syntaxes except Manchester syntax offer facilities to do so :

*vin:Bancroft rdfs:type owl:NamedIndividual.*

*vin:Winery rdfs:type owl:Class .*

*vin:adjacentRegion rdfs:type owl:ObjectProperty .*

*vin:yearValue rdfs:type owl:DatatypeProperty .*

# Ontology mapping

- The Semantic Web is distributed; so is ontology construction.
  - It is common for ontologies to use different names for the same concept, property, or individual.
  - It is common usage to develop ontologies in several parts, which then need to be **mapped** together.
- Equivalence declarations can be used for that purpose : **equivalentClass** for classes, **equivalentProperty** for properties and **sameAs** for individuals :

*:Mary owl:sameAs otherOnt:MaryBrown .*

*:Adult owl:equivalentClass otherOnt:Grownup .*

*:hasChild owl:equivalentProperty otherOnt:child .*

- To make sure individuals are different, this must be specified.
  - **OWL does not have the unique name assumption.**

*:John owl:differentFrom :Bill .*

# Agenda

- 1 Why OWL ?
- 2 Species of OWL
- 3 OWL-DL
- 4 OWL 2
- 5 OWL 2 Semantics

# OLW 2

- **OLW 1** has been successful; its usage has shown additional needs :
  - A suitable set of built-in datatypes (OLW 1 still relied on XML-Schema datatypes);
  - Additional features identified by users for which effective reasoning algorithms are now available.
  
- **OLW 2** was adopted as W3C recommendation in 2009, backward compatible :
  - All OWL 1 ontologies remain valid OWL2 ontologies, with identical inferences in all practical cases.



# OLW 2 relationship to OWL 1

- The overall structure of OWL 2 is very similar to OWL 1. Almost all OWL 2 building blocks were present in OWL 1, sometimes in a different name.
- OWL 2 adds new features with respect to OWL 1 :
  - **Syntactic sugar** : doesn't change expressiveness or complexity but makes patterns easier to write and allows for more efficient processing in reasoner : disjoint union, disjoint classes (cf. chapter 5), negative assertions.
  - **New constructs for properties** : cardinality restrictions, property chain inclusion, new axioms (reflexive, asymmetric ...).
  - **Extended datatypes** : richer set of datatypes (e.g. various types of numbers) and datatype restrictions.
  - **Punning** : the same name can be used as class and as instance (*dog* is a class and an instance of *species*).  
Note : OWL 2 DL treats the two usages as totally different instances of the same name, to preserve decidability.
  - **Extended annotations** : OWL1 could only annotate the ontology. OWL 2 can annotate classes and properties.
  - **Other minor features.**

# OWL 2 Profiles

Complexity remains a key factor. OWL 2 offers three distinct **tractable** profiles:

- **EL**: fast reasoning services (**ptime**) for large ontologies (classes, properties).
  - Many applications, in particular in life sciences, have large ontologies : SNOMED, GO ...
  - They need to represent complex entities, to propagate properties (e.g., location of diseases ...).
  - EL is designed for such ontologies with a large conceptual / taxonomy part.
  
- **QL**: Efficient query answering using RDBMs via SQL.
  - Conjunctive query answering in **logspace** wrt size of data; consistency and subsumption reasoning in **ptime**.
  - For applications needing inter-operability with database technologies and tools.
  - QL is useful for large datasets already stored in RDBs.
  
- **RL**: can be implemented using rule-based technologies (rule-extended DBMSs, Prolog ...)
  - Fast reasoning services (**ptime**).
  - For applications concerned with inter-operability with rule engines operating at RDF level.
  - RL is useful for managing large datasets of RDF triples which can be enriched with rules.

# Compatibility of reasoners

- ❑ Every conforming OWL 2 DL reasoner is also a conforming reasoner for OWL 2 EL, OWL 2 RL, and OWL 2 QL !
- ❑ But they may differ in performance as the OWL 2 DL reasoner is tuned for a more general set of cases.

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# OLW Semantics

- Two semantics are defined for OWL 2 :

## 1. Direct semantics:

- Model-theoretic semantics similar to DL **SROIQ**, extended for datatypes and punning.

Due to these extensions the direct semantics has received a separate formal definition. We will satisfy ourselves to summarize the mapping between OWL 2 DL and description logics (mapping table next slide).

- Assigns meaning to **OWL 2 DL** ontologies (those meeting the restrictions necessary to be translated into DL).
- Also provides semantics for **OWL 1 Lite** and **OWL 1 DL** ontologies and **OWL 2** profiles.
- As description logics, OWL uses the Open World assumption.

## 2. RDF-based semantics:

- Assigns RDF-based meaning to all OWL 2 (full) ontologies;
- For an OWL 2 DL ontology, inferences based on direct semantics are still valid using RDF-based semantics.
- Will not be covered in this course.

# Mapping between OWL and description logics

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Abstract Syntax	DL Syntax
Descriptions ( $C$ )	
$A$	$A$
owl:Thing	$\top$
owl:Nothing	$\perp$
intersectionOf( $C_1 \dots C_n$ )	$C_1 \sqcap \dots \sqcap C_n$
unionOf( $C_1 \dots C_n$ )	$C_1 \sqcup \dots \sqcup C_n$
complementOf( $C$ )	$\neg C$
oneOf( $o_1 \dots o_n$ )	$\{o_1\} \sqcup \dots \sqcup \{o_n\}$
restriction( $R$ someValuesFrom( $C$ ))	$\exists R.C$
restriction( $R$ allValuesFrom( $C$ ))	$\forall R.C$
restriction( $R$ hasValue( $o$ ))	$R : o$
restriction( $R$ minCardinality( $n$ ))	$\geq n R$
restriction( $R$ maxCardinality( $n$ ))	$\leq n R$
restriction( $U$ someValuesFrom( $D$ ))	$\exists U.D$
restriction( $U$ allValuesFrom( $D$ ))	$\forall U.D$
restriction( $U$ hasValue( $v$ ))	$U : v$
restriction( $U$ minCardinality( $n$ ))	$\geq n U$
restriction( $U$ maxCardinality( $n$ ))	$\leq n U$
Data Ranges ( $D$ )	
$D$	$D$
oneOf( $v_1 \dots v_n$ )	$\{v_1\} \sqcup \dots \sqcup \{v_n\}$
Object Properties ( $R$ )	
$R$	$R$
inv( $R$ )	$R^-$
Datatype Properties ( $U$ )	
$U$	$U$
Individuals ( $o$ )	
$o$	$o$
Data Values ( $v$ )	
$v$	$v$

Fig. 14.2. OWL DL Descriptions, Data Ranges, Properties, Individuals, and Data Values

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Abstract Syntax	DL Syntax
Class( $A$ partial $C_1 \dots C_n$ )	$A \sqsubseteq C_1 \sqcap \dots \sqcap C_n$
Class( $A$ complete $C_1 \dots C_n$ )	$A \equiv C_1 \sqcap \dots \sqcap C_n$
EnumeratedClass( $A$ $o_1 \dots o_n$ )	$A \equiv \{o_1\} \sqcup \dots \sqcup \{o_n\}$
SubClassOf( $C_1$ $C_2$ )	$C_1 \sqsubseteq C_2$
EquivalentClasses( $C_1 \dots C_n$ )	$C_1 \equiv \dots \equiv C_n$
DisjointClasses( $C_1 \dots C_n$ )	$C_i \sqcap C_j \sqsubseteq \perp, i \neq j$
Datatype( $D$ )	
ObjectProperty( $R$ super( $R_1$ )...super( $R_n$ ))	$R \sqsubseteq R_i$
domain( $C_1$ )...domain( $C_m$ )	$\geq 1 R \sqsubseteq C_i$
range( $C_1$ )...range( $C_\ell$ )	$\top \sqsubseteq \forall R.C_i$
[inverseOf( $R_0$ )]	$R \equiv R_0^-$
[Symmetric]	$R \equiv R^-$
[Functional]	$\top \sqsubseteq \leq 1 R$
[InverseFunctional]	$\top \sqsubseteq \leq 1 R^-$
[Transitive]	$Tr(R)$
SubPropertyOf( $R_1$ $R_2$ )	$R_1 \sqsubseteq R_2$
EquivalentProperties( $R_1 \dots R_n$ )	$R_1 \equiv \dots \equiv R_n$
DatatypeProperty( $U$ super( $U_1$ )...super( $U_n$ ))	$U \sqsubseteq U_i$
domain( $C_1$ )...domain( $C_m$ )	$\geq 1 U \sqsubseteq C_i$
range( $D_1$ )...range( $D_\ell$ )	$\top \sqsubseteq \forall U.D_i$
[Functional]	$\top \sqsubseteq \leq 1 U$
SubPropertyOf( $U_1$ $U_2$ )	$U_1 \sqsubseteq U_2$
EquivalentProperties( $U_1 \dots U_n$ )	$U_1 \equiv \dots \equiv U_n$
AnnotationProperty( $S$ )	
OntologyProperty( $S$ )	
Individual( $o$ type( $C_1$ )...type( $C_n$ ))	$o \in C_i$
value( $R_1$ $o_1$ )...value( $R_n$ $o_n$ )	$\langle o, o_i \rangle \in R_i$
value( $U_1$ $v_1$ )...value( $U_n$ $v_n$ )	$\langle o, v_i \rangle \in U_i$
SameIndividual( $o_1 \dots o_n$ )	$\{o_1\} \equiv \dots \equiv \{o_n\}$
DifferentIndividuals( $o_1 \dots o_n$ )	$\{o_i\} \sqsubseteq \neg\{o_j\}, i \neq j$

Fig. 14.3. OWL DL Axioms and Facts

(source Horrocks et al. 2007. These tables use abstract syntax. The mapping with the Turtle syntax can be found in the [OWL 2 Primer](#).)

# Summary

- ❑ OWL aims to integrate the flexibility and linked data access provided by RDF graphs with the precise semantics of description logics.
- ❑ This is only possible with restrictions on RDF constructs, in particular the constructs representing a class and a property.
- ❑ These restrictions led to the OWL DL sublanguage, which can be mapped into description logics and for which efficient reasoners exist.
- ❑ The full flexibility of RDF is still available in OWL Full, for which, however, no reasoner covering the entire language exists.
- ❑ OWL 2 DL the most expressive decidable ontology language (corresponding to description logic  $\mathcal{SROIQ}(\mathcal{D})$ ).
- ❑ 3 additional tractable simplified languages are proposed : OWL2 EL, RL and QL.
- ❑ OWL is the language of references for ontologies for the semantic web, supported by an array of reasoners and other tools.

# References

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THANK YOU