

# ELEN0037

## Microelectronics

### Tutorials

Pouyan Ebrahimbabaie, Vinayak Pachkawade, Thomas Schmitz

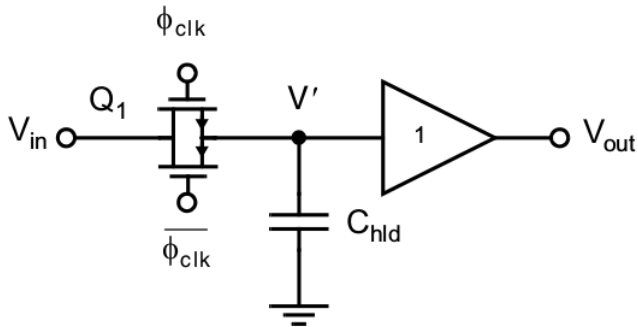
With special thanks to Vincent Pierlot

University of Liège - Montefiore Institute  
EMMI Unit: Electronics, Microsystems, Measurements, and Instrumentation

Tutorial 3: Sample and Holds, Switched-Capacitor circuits

## Exercise 1 (1st, P8.2/2nd, P11.4)

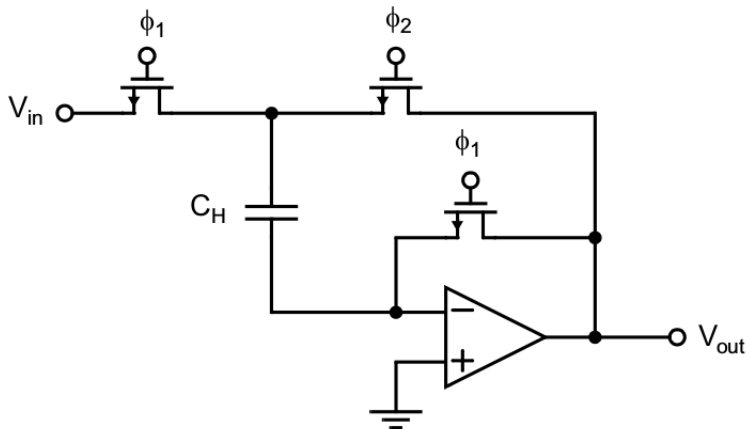
In the following S/H circuit, assume  $V_{in}$  is a  $20\text{ MHz}$  sinusoid with a  $2\text{ V}_{pp}$  amplitude. Also assume that  $\phi_{clk}$  is a  $100\text{ MHz}$  square wave having a peak amplitude of  $\pm 2.5\text{ V}$  with rise and fall times of  $1.5\text{ ns}$ . What is the maximum time difference between the turn-off times of the n-channel and p-channel transistors?<sup>1</sup> Ignore the body effect ( $V_{tn} = 0.8\text{ V}$ ,  $V_{tp} = -0.9\text{ V}$ ).



<sup>1</sup> $|\Delta\phi|_{max} = 2.1\text{ V}$ ,  $\Delta t_{max} = 0.63\text{ ns}$

## Exercise 2 (1st, P8.6/2nd, P11.8)

Assume the opamp of the following S/H circuit has a finite gain of  $A$ , and offset voltage  $V_{offset}$ . Derive the output voltage in terms of  $V_{in}$ ,  $A$ , and  $V_{offset}$  during hold mode (i.e., when  $\phi_2$  is high).<sup>2</sup>

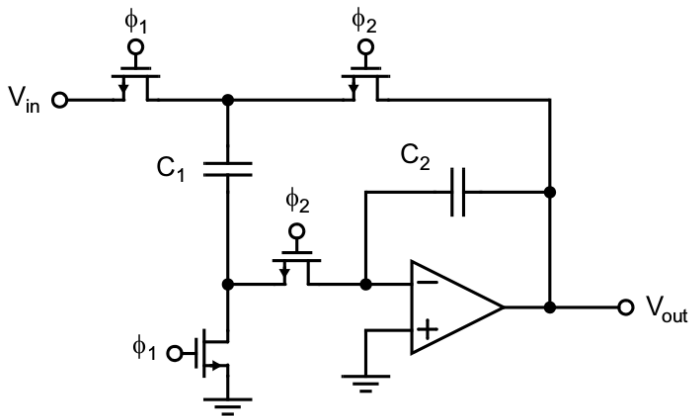


---

$$^2 V_{out} = \frac{A}{A+1} V_{in} + \frac{A}{(A+1)^2} V_{offset}$$

## Exercise 3 (1st, P8.7/2nd, P11.9)

Derive the frequency-domain transfer function of the following S/H circuit (use  $z = e^{j\omega T}$ ), and find the cut-off frequency  $f_{-3dB}$ . Make the assumption that  $e^{j\omega T} \cong 1 + j\omega T$  for  $\omega T \ll 1$ .<sup>3</sup>

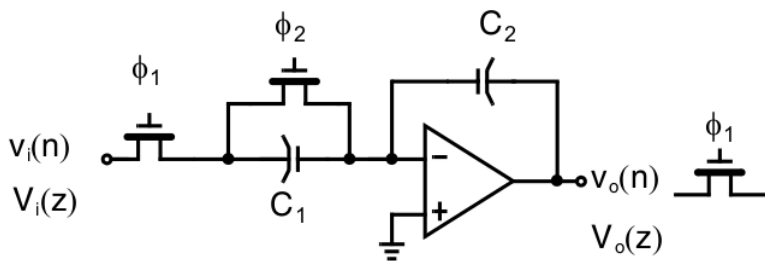


---

$$^3 H(z) = \frac{z^{-1}}{1 + C_2/C_1(1-z^{-1})}, \quad f_{-3dB} = \frac{1}{2\pi} \frac{C_1}{C_2} f_s$$

## Exercise 4 (1st, P10.2/2nd, P14.4)

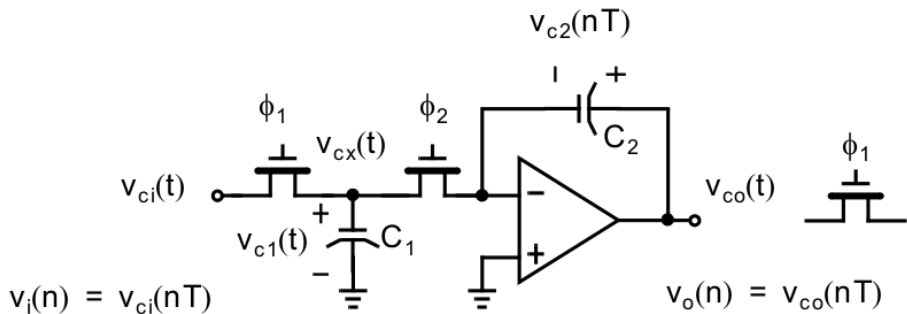
Ignoring the effect of parasitic capacitances, find the discrete-time transfer function of the following switched-capacitor circuit.<sup>4</sup>



<sup>4</sup> $H(z) = - (C_1/C_2) \frac{1}{1-z^{-1}}$  (delay-free inverting integrator)

## Exercise 5 (1st, P10.4/2nd, P14.6)

Compute the transfer function of the following discrete-time integrator, when the opamp has a finite gain of  $A$ .<sup>5</sup> Also show that this transfer function has a DC gain of  $-A$  and a pole that is located slightly to the left of 1.



$${}^5 H(z) = -\left(\frac{C_1}{C_2}\right) \left(\frac{A}{A+1}\right) \frac{z^{-1}}{1 - \left(1 - \frac{C_1}{C_2(A+1)}\right) z^{-1}}, \quad z_p = 1 - \frac{C_1}{C_2} \frac{1}{A+1} \lesssim 1$$